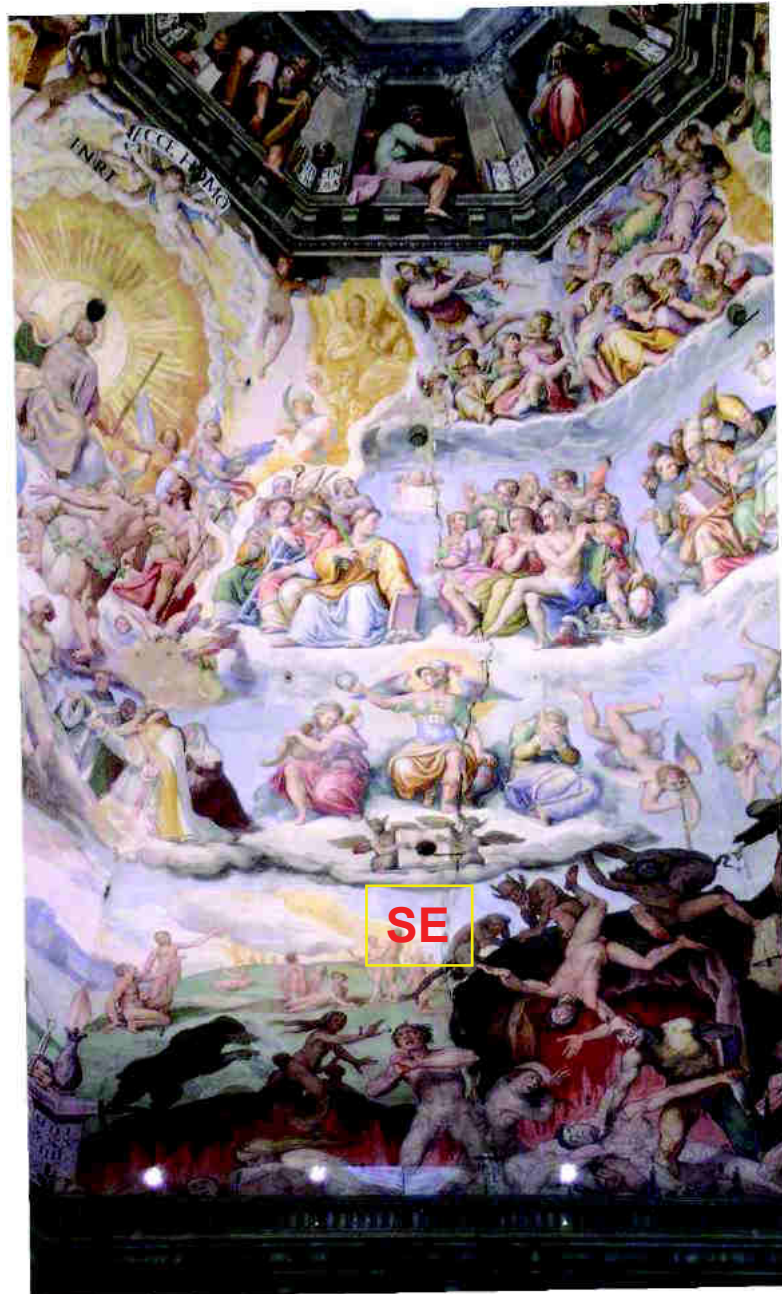
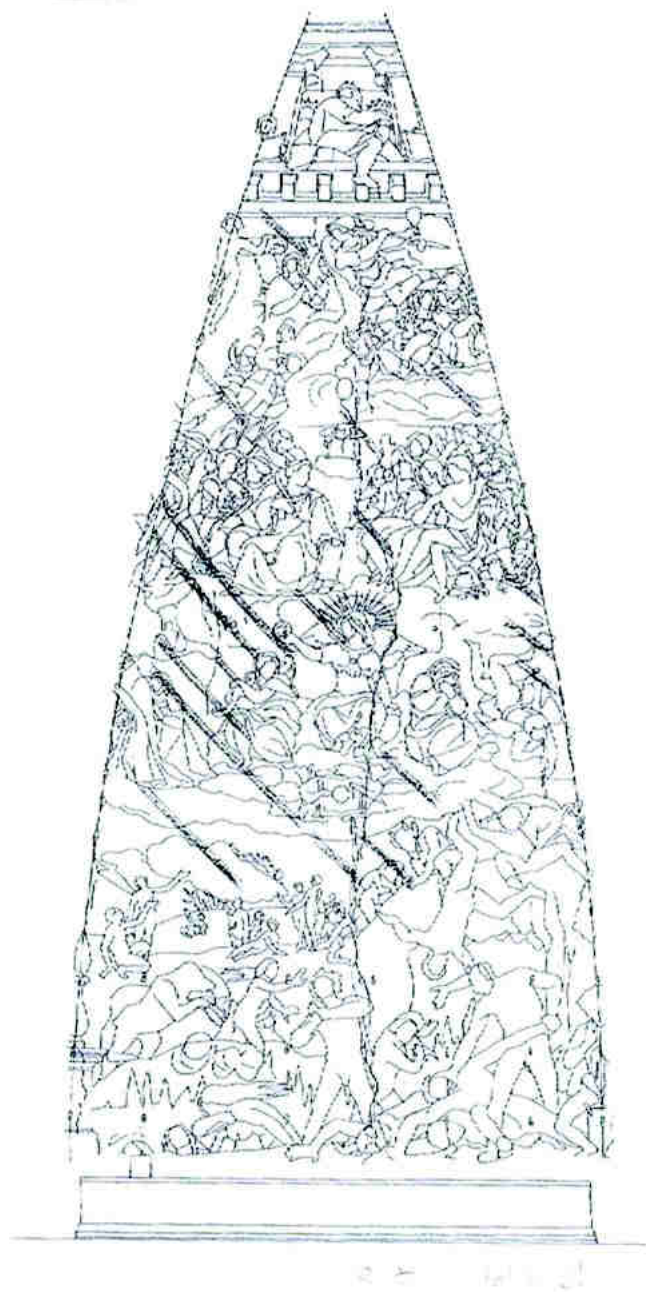




**NE main meridional crack**  
**External view**



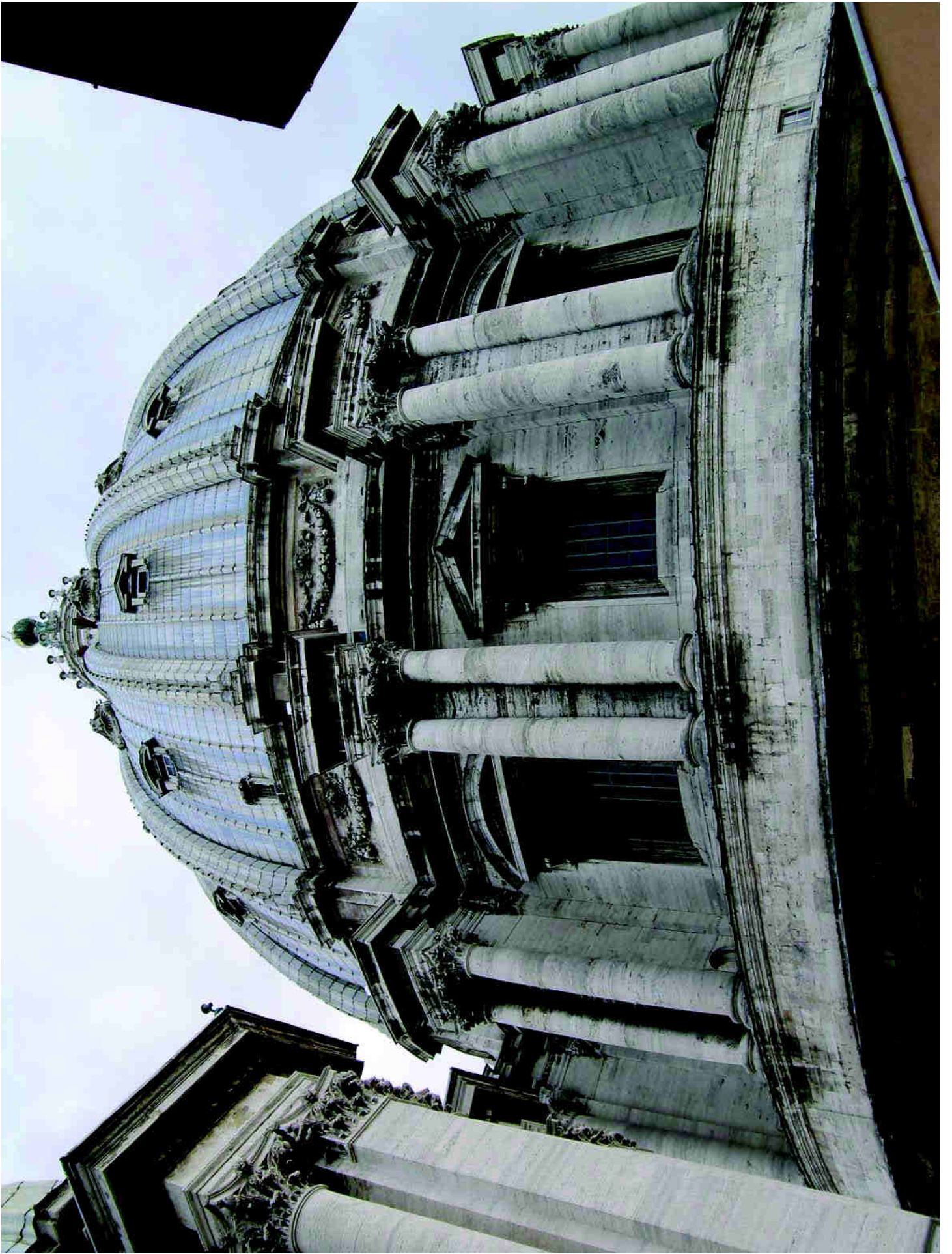


# *San Pietro*

*J. Della Porta 1590*

*Ø, 42.84 m*









# St. Peter dome in Rome (built 1590) Development of cracks (1742)

**P A R E R E**  
**D I T R E**  
**M A T T E M A T I C I**  
 Sopra i danni, che si sono trovati  
**N E L L A C U P O L A**  
**D I S. P I E T R O**  
 Sul fine dell'Anno MDCCLII.  
**D A T O P E R O R D I N E**  
**D I N O S T R O S I G N O R E**  
**P A P A B E N E D E T T O X I V.**

(Boscovich, Le Soeur e Jacquier, 1742)

**Insufficienza dei contrafforti**  
**Rotture per taglio**  
**con fessure inclinate**

1 palmo = 12 once = 22.3 cm  
 1 oncia = 5 minuti = 1.86 cm  
 1 minuto = 0.371 cm

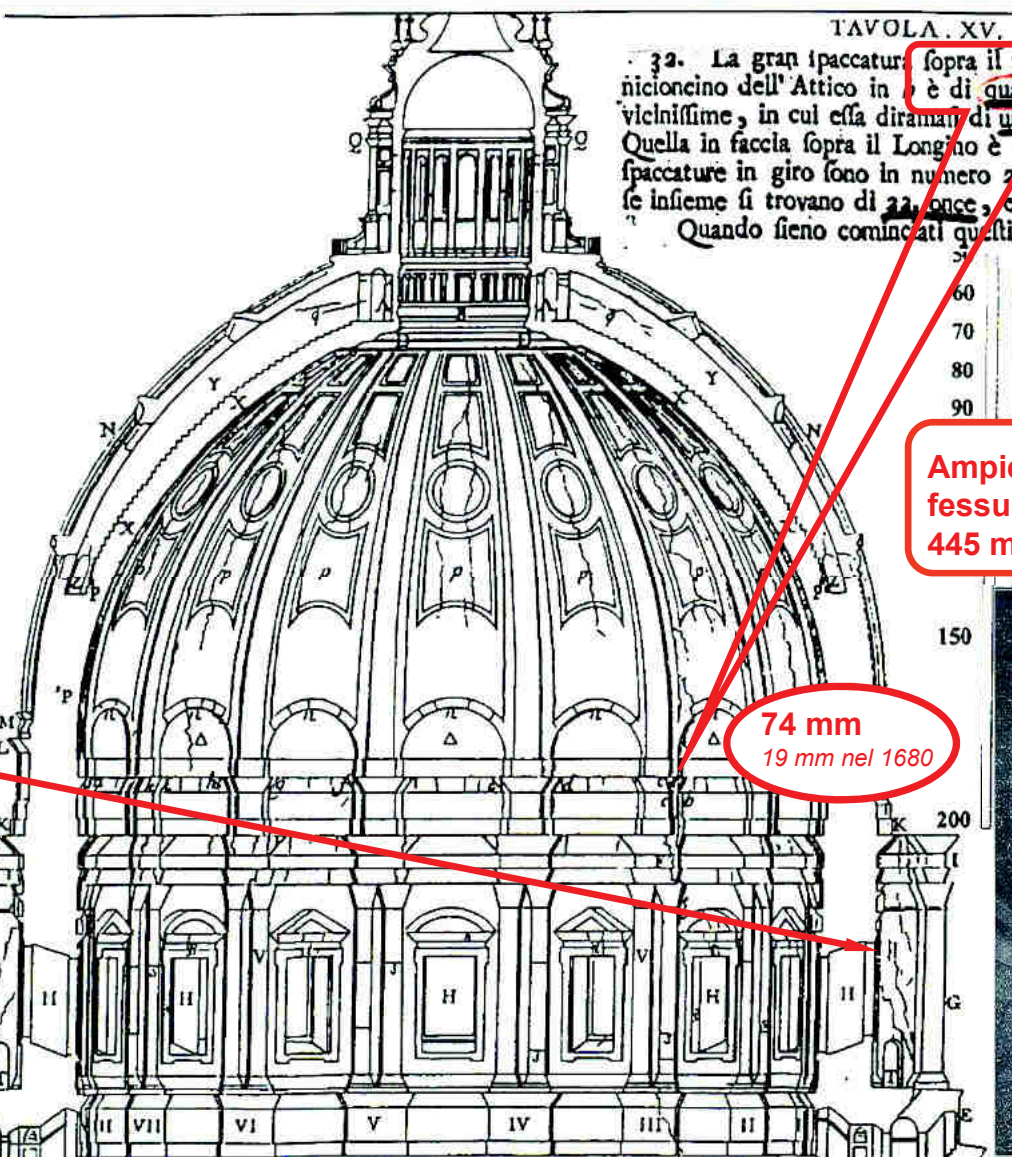


TAVOLA . XV.

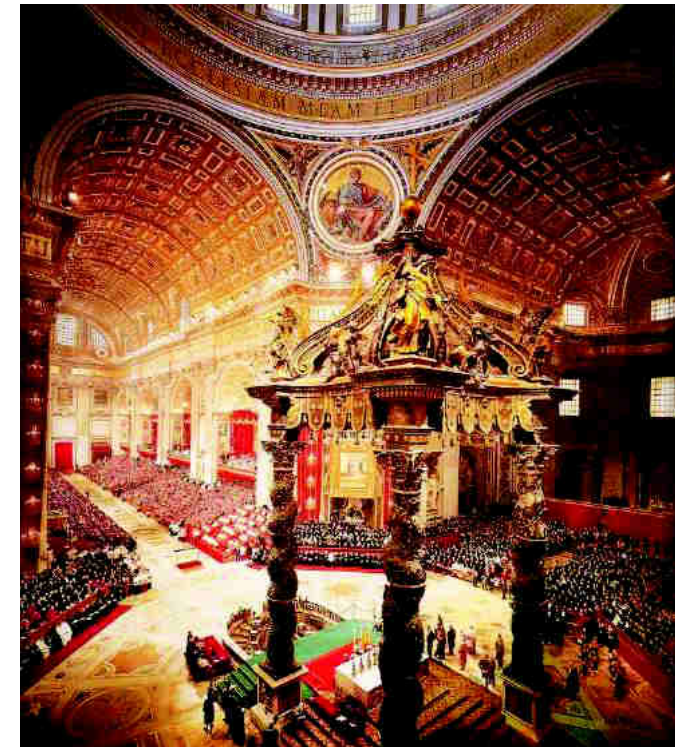
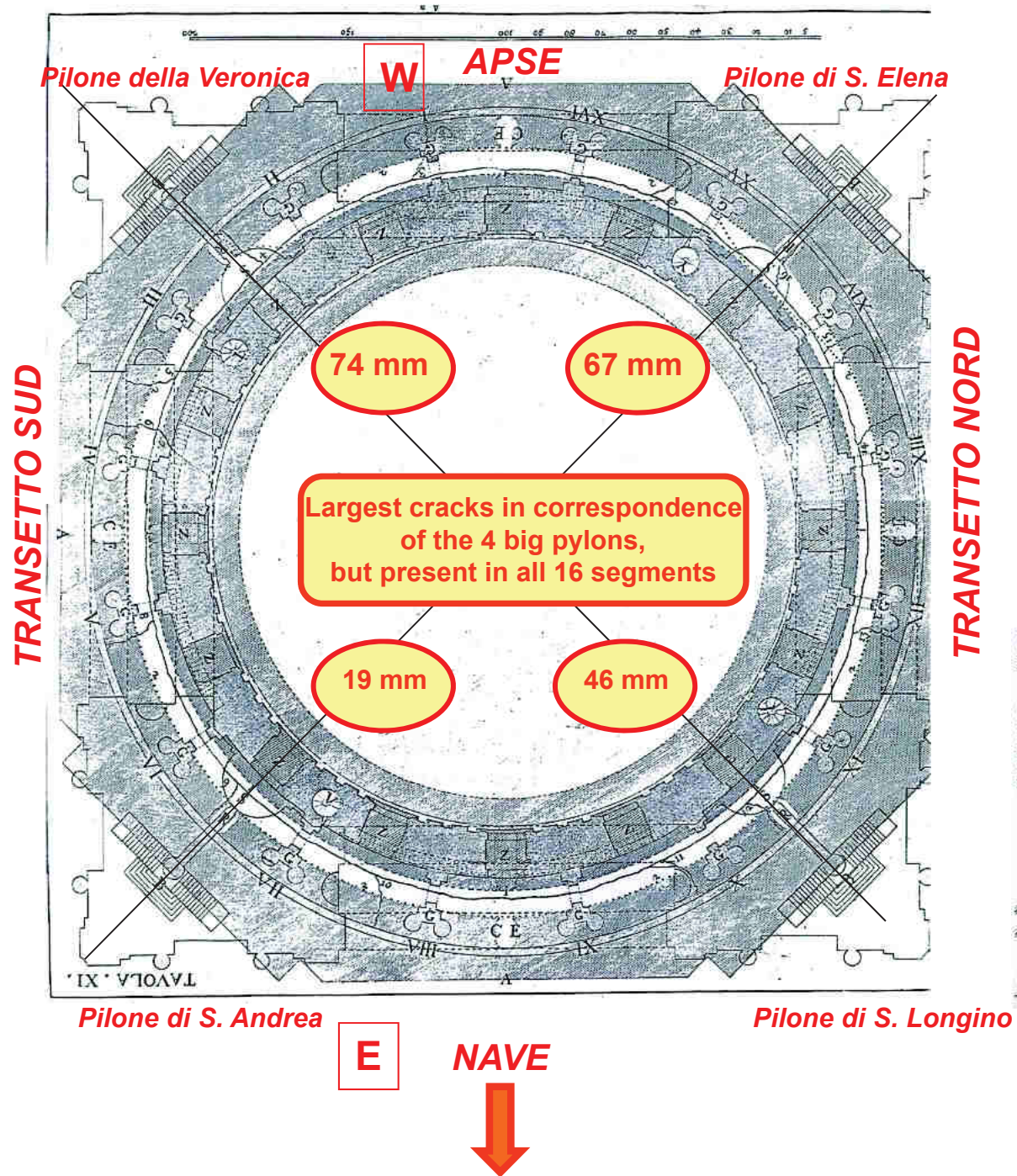
32. La gran spaccatura sopra il pilone della Veronica sul cornicioncino dell'Attico in è di quattro once, e vene sono due vicinissime, in cui essa diraman di un'oncia e mezza tra tutte due. Quella in faccia sopra il Longino è di due once e mezza: Ivi le spaccature in giro sono in numero 27., e tanto grosse, che messe insieme si trovano di 22 once, e poco più sù di 24. Quando sieno cominciati questi danni non si sa con certezza.

**Ampiezza complessiva**  
**fessure sul perimetro**  
**445 mm**

**74 mm**  
 19 mm nel 1680



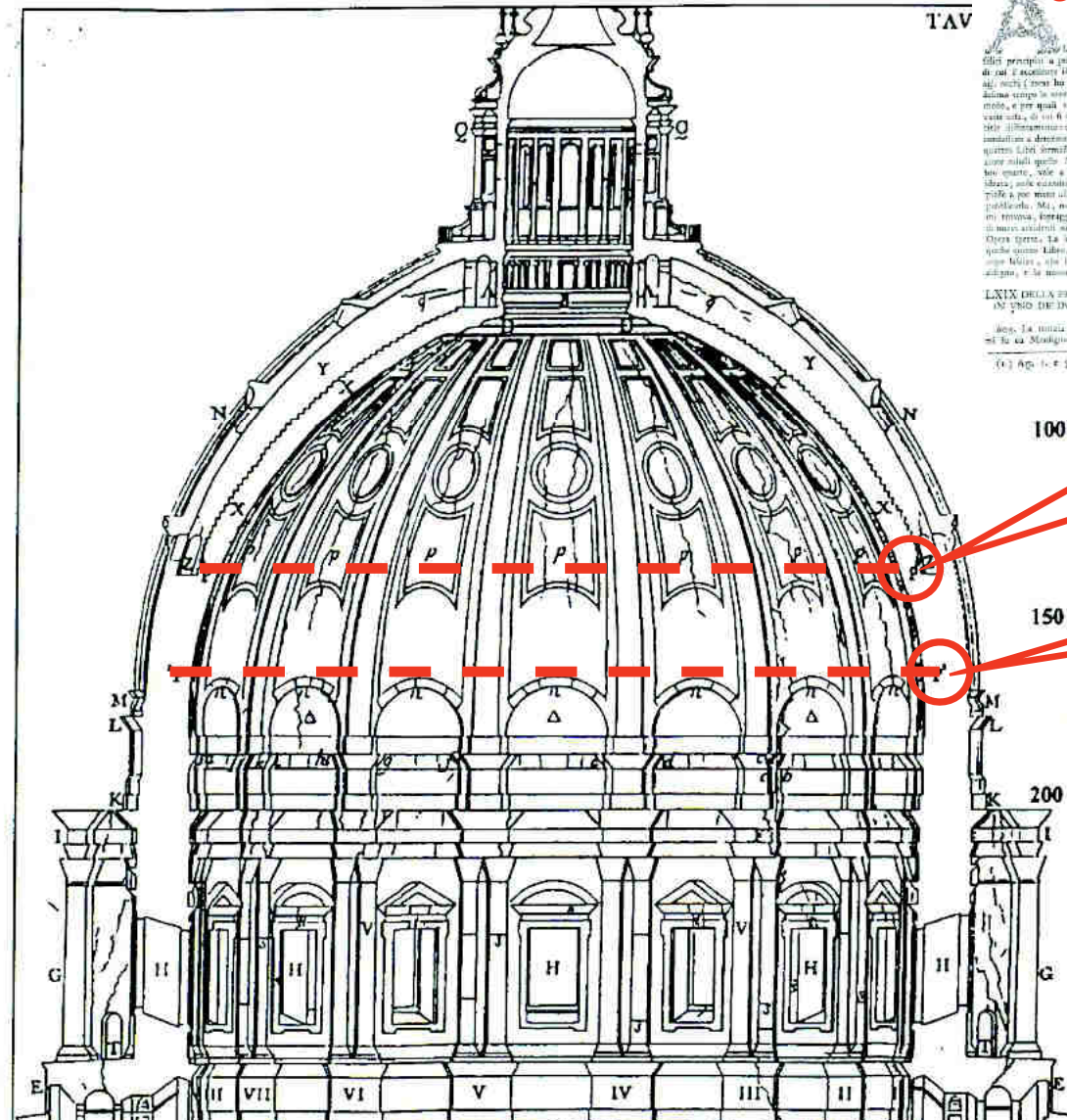
**Beltrami**  
 1929





The upper iron ring resulted to be broken during the inspections by Poleni for the placement of the additional rings

MEMORIE ISTORICHE  
DELLA  
GRAN CVPOLA  
DEL  
TEMPIO VATICANO  
LIBRO QUINTO.  
G. Poleni, Padova 1748



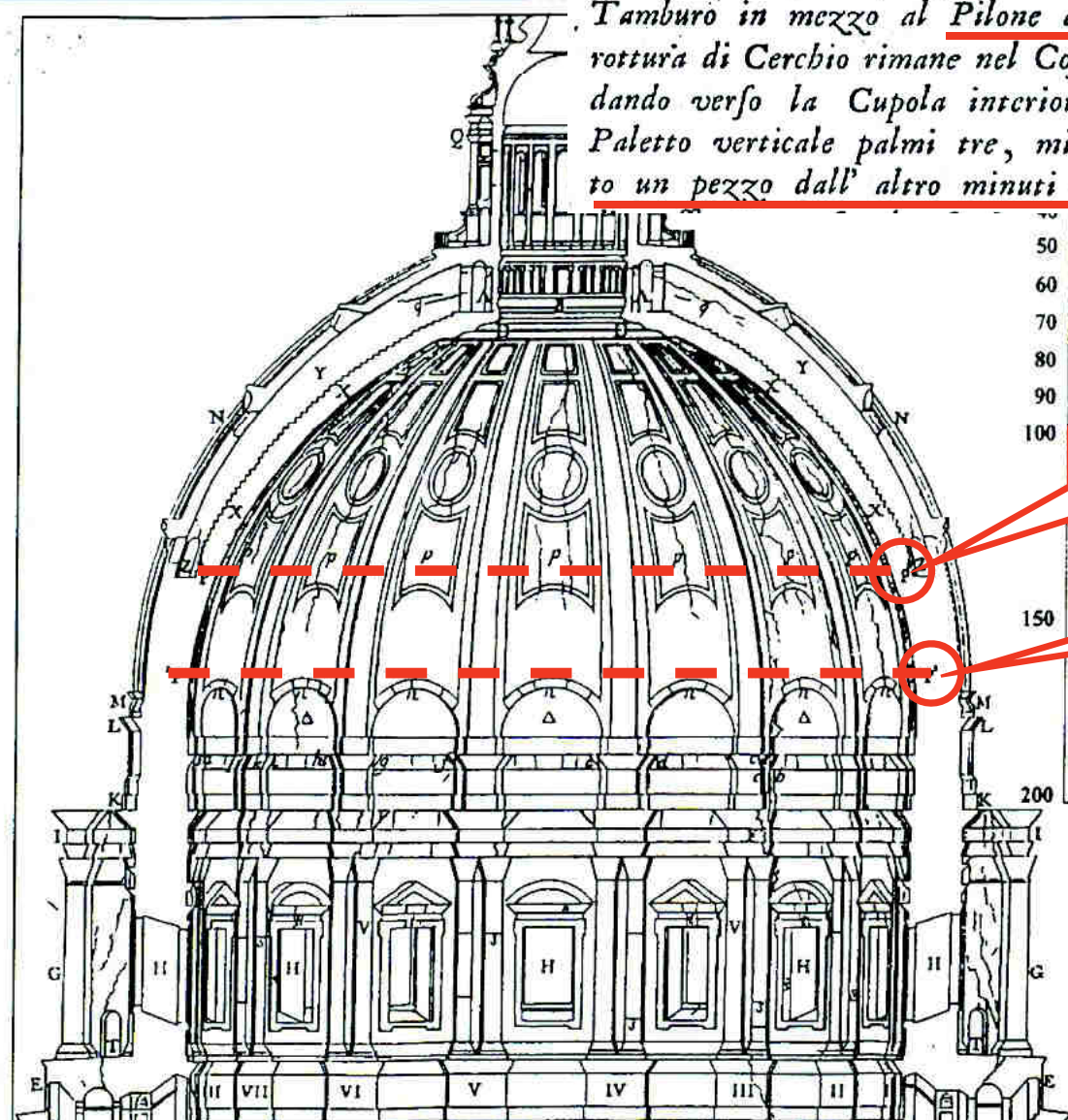
100  
2nd iron ring  
broken in correspondence  
of the Pilon della Veronica

150  
1st iron ring  
undamaged?

TAV  
PREFAZIONE  
ALLORA questo con altri  
della prefazione a parlare del  
di cui l'eccezione era un  
agli occhi (non ha l'altre  
sulla cima se non come se  
modo, e per quali sia  
vasta sala, di cui 6  
della differenza e la  
medesima a discesa  
quattro libri sermone  
lungo molti quelle  
due mura, vide a  
libro, può essere  
rispetto a per  
particolare. Ma,  
in tempo, forse  
in un altro stato  
Ora opera. La  
come Mura, e  
almeno alla  
LXXIX DELLA PRIMA  
DE UNO DE DUE  
100. La  
100. Il  
100.

The upper iron ring resulted to be broken during the inspections by Poleni for the placement of the additional rings

*Nel medemo Cerchione si è ritrovata altra seconda rottura nel sito corrispondente sulla Fenestra del Tamburo in mezzo al Pilone della Veronica, quale rottura di Cerchio rimane nel Costolone sinistro ( guardando verso la Cupola interiore ) in distanza dal Paletto verticale palmi tre, minuti cinque, distaccato un pezzo dall' altro minuti quattordici, e mezzo*



5,4 cm

2nd iron ring  
broken in correspondence  
of the Pilone della Veronica

1st iron ring  
undamaged?

# Insertions of new iron rings

G. Poleni e L. Vanvitelli 1743-48

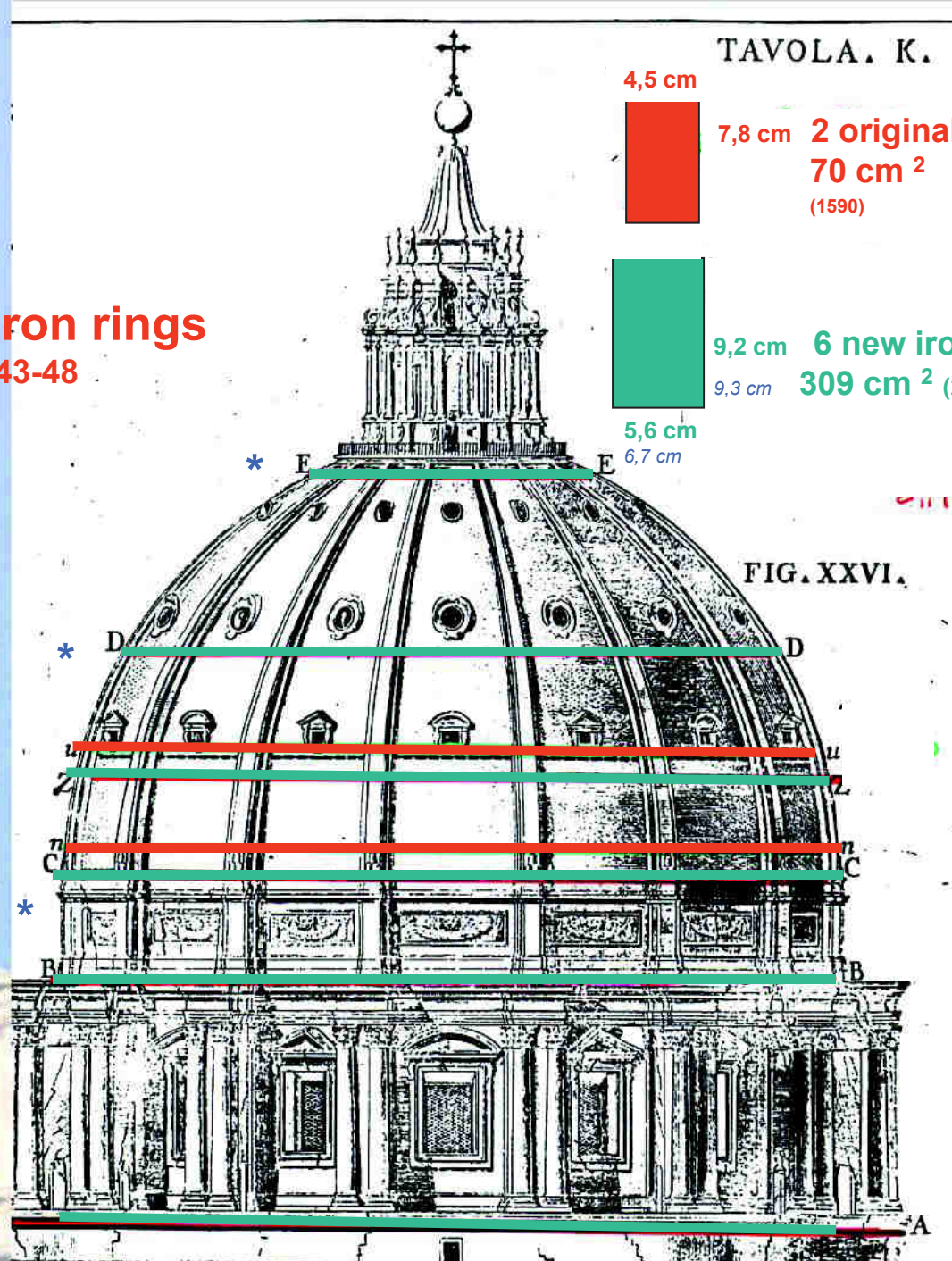


TAVOLA. K.

4,5 cm

7,8 cm **2 original iron rings**  
**70 cm<sup>2</sup>**  
 (1590)



9,2 cm **6 new iron rings**  
 9,3 cm **309 cm<sup>2</sup>** (210 cm<sup>2</sup> being active)

5,6 cm  
 6,7 cm

FIG. XXVI.

Posizione delle cerchiature  
 proposta dai Tre Mattematici

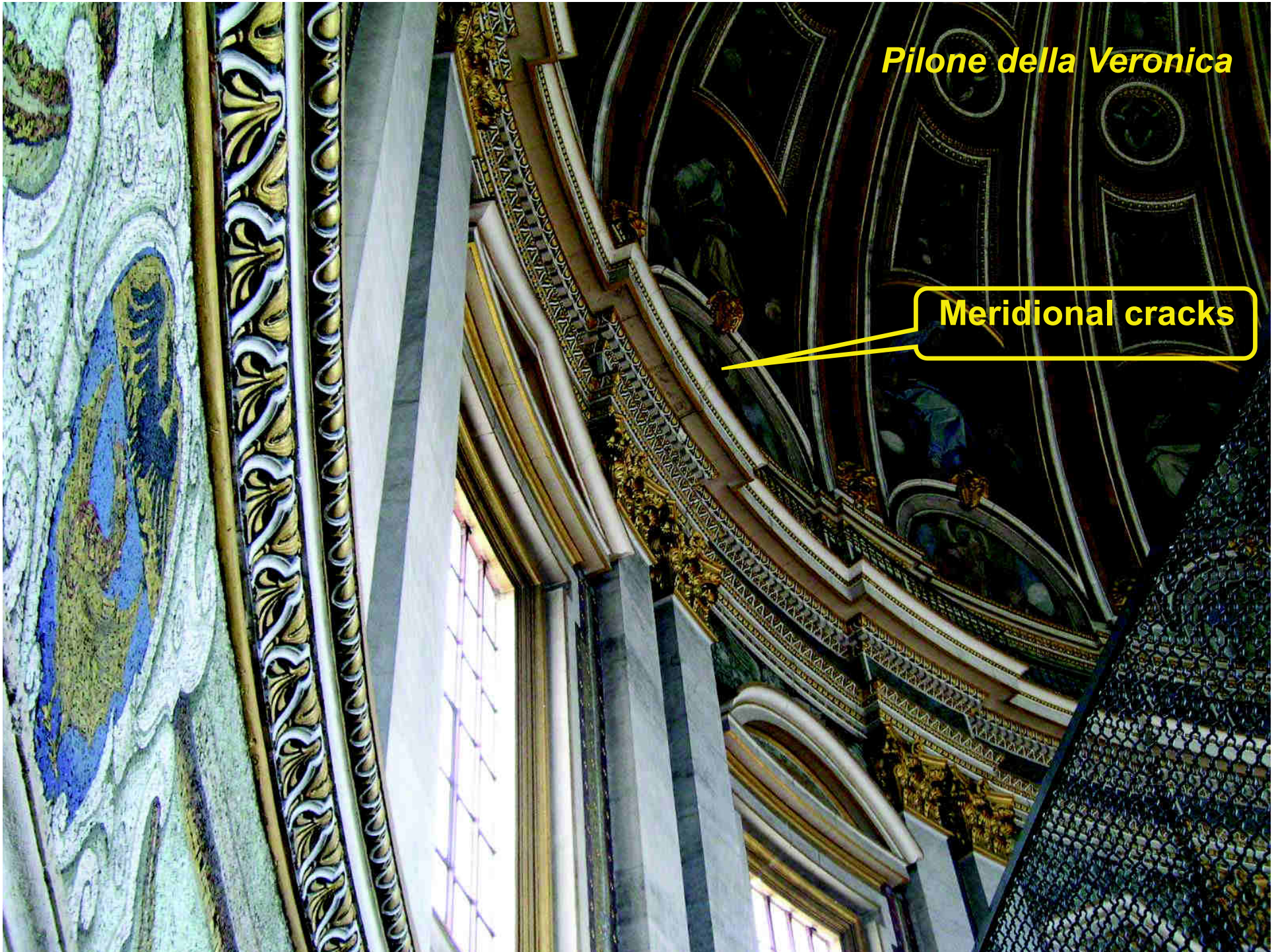
Cerchi esterni \*

Cerchio interno \*

\* \*

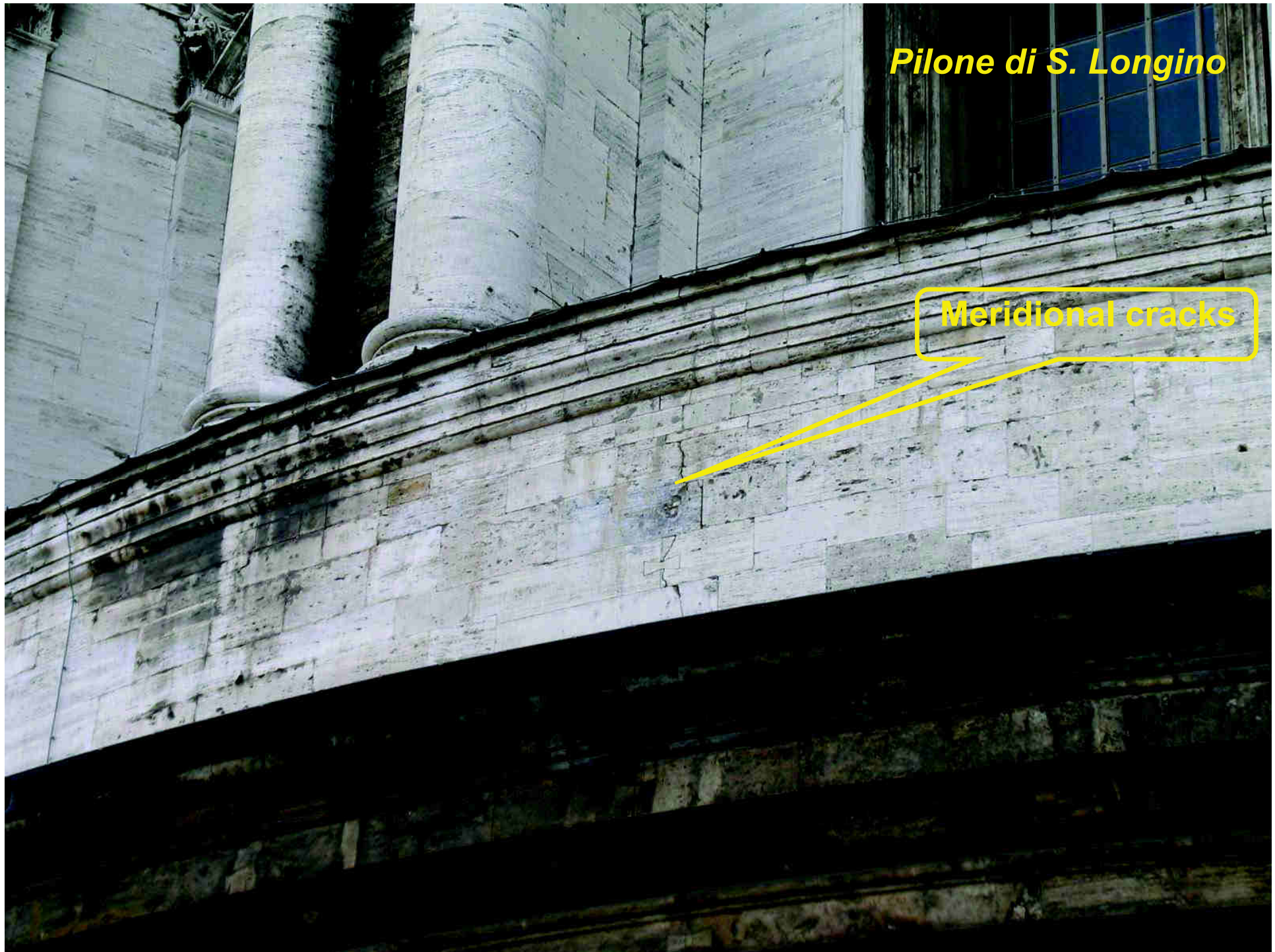
*Pilone della Veronica*

Meridional cracks



*Pilone di S. Longino*

Meridional cracks



*Pilone di S. Longino*

MAIR J856

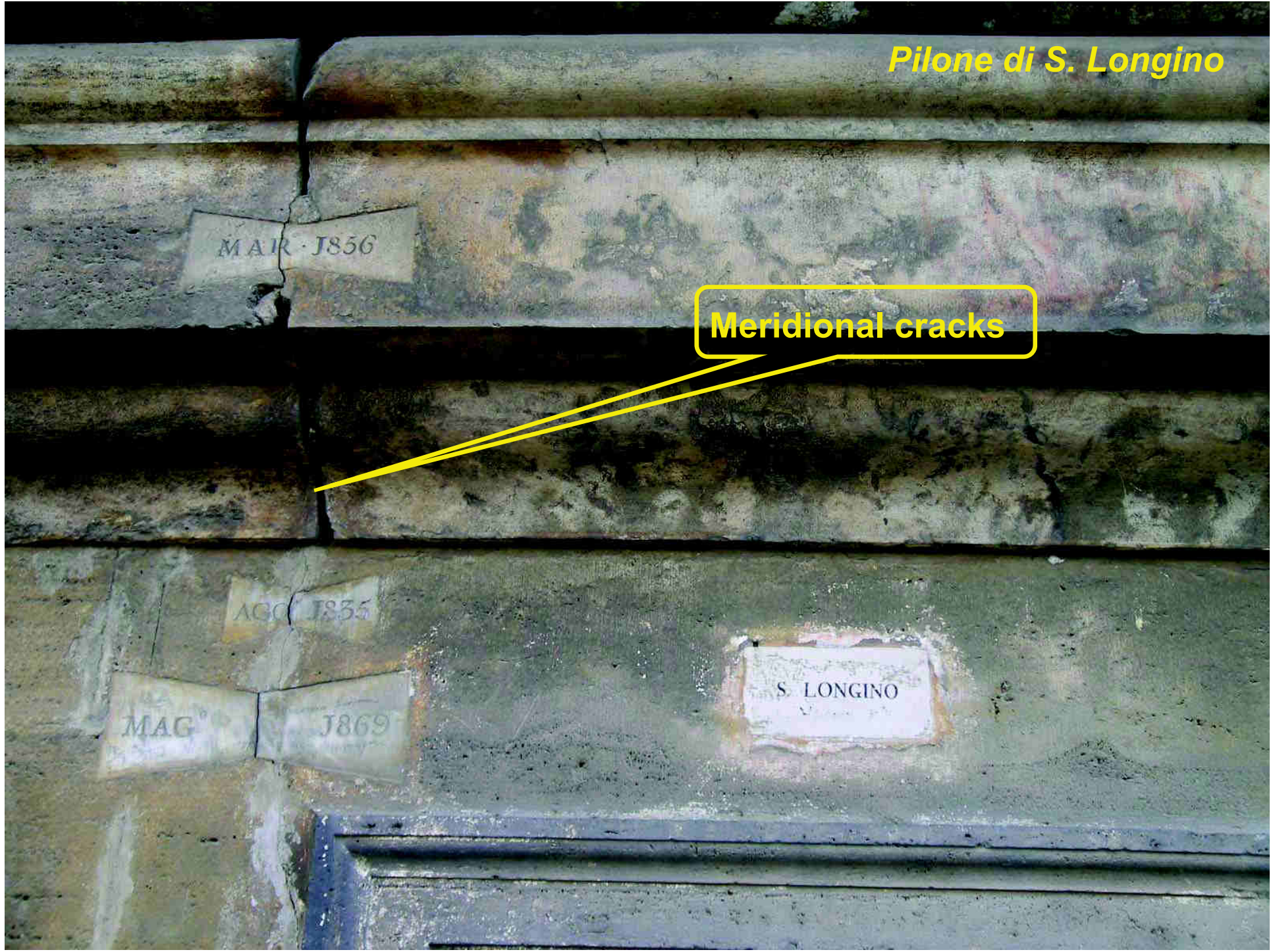
Meridional cracks

AGG J855

MAG

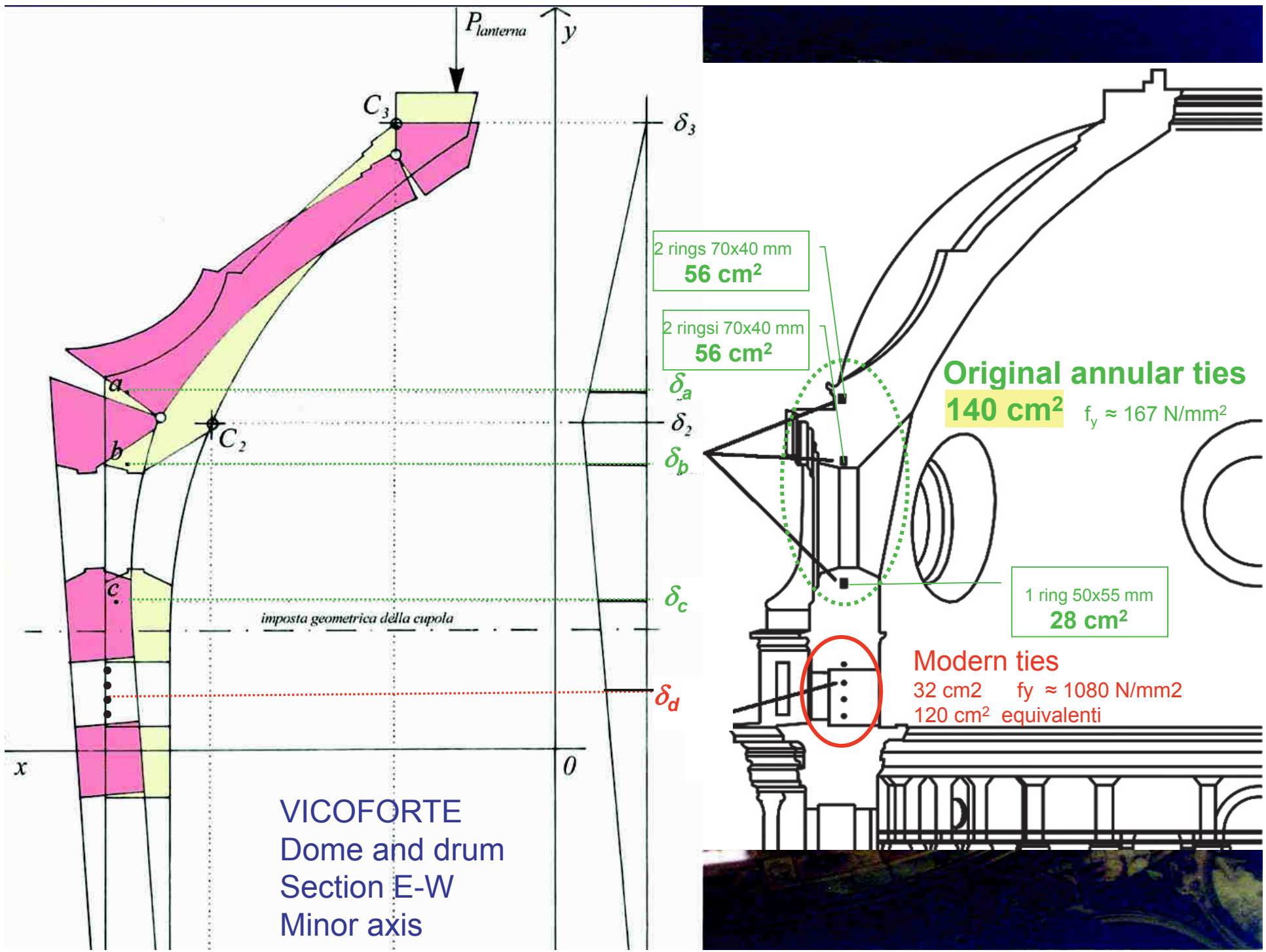
J869

S. LONGINO





**VICOFORTE**  
**Original iron rings**



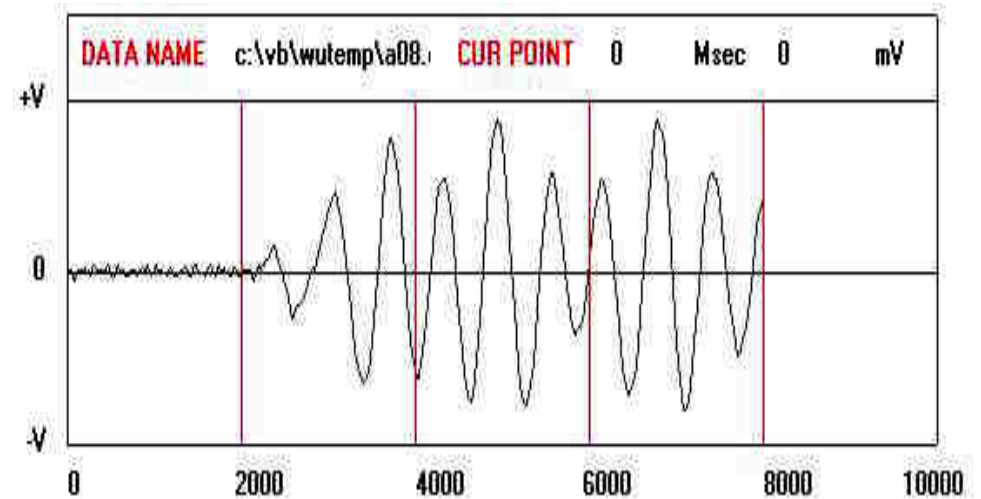


# Original iron rings (Gallo 1731)

## Details

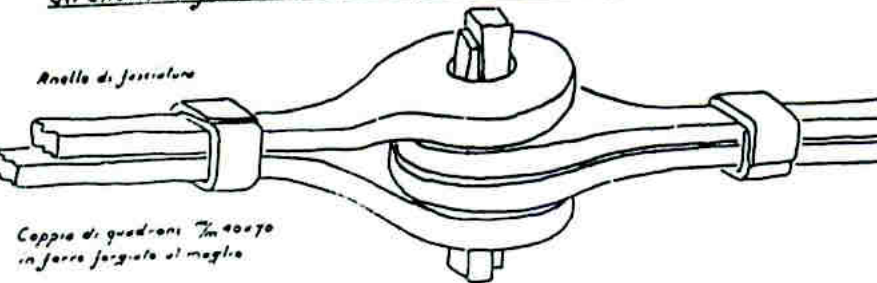


## Continuity checks by sonic testing



*Gli anelli di fasciatura della Cupola dell'Arch. Inq. Francesco Gallo - 1731*

*Anello di fasciatura*



*Coppia di quadranti Tm 40070  
in ferro forgiato al maglio*

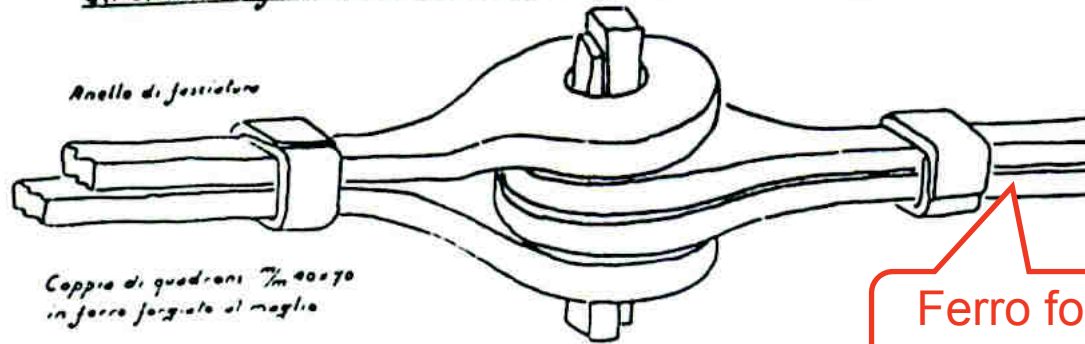
*Giunite con dischi terminali forgiati e  
chiusure a uncini di collegamento e tensione*

# Fastening of circular rings

## Vicoforte

### F. Gallo 1731 Original rings

*Gli anelli di fasciatura della Cupola dell'Arch. Ing. Francesco Gallo - 1731*



*Giunti con dischi terminali forgiati e chiodate a cunei di collegamento e tensione*

Ferro forgiato  
40x70 mm

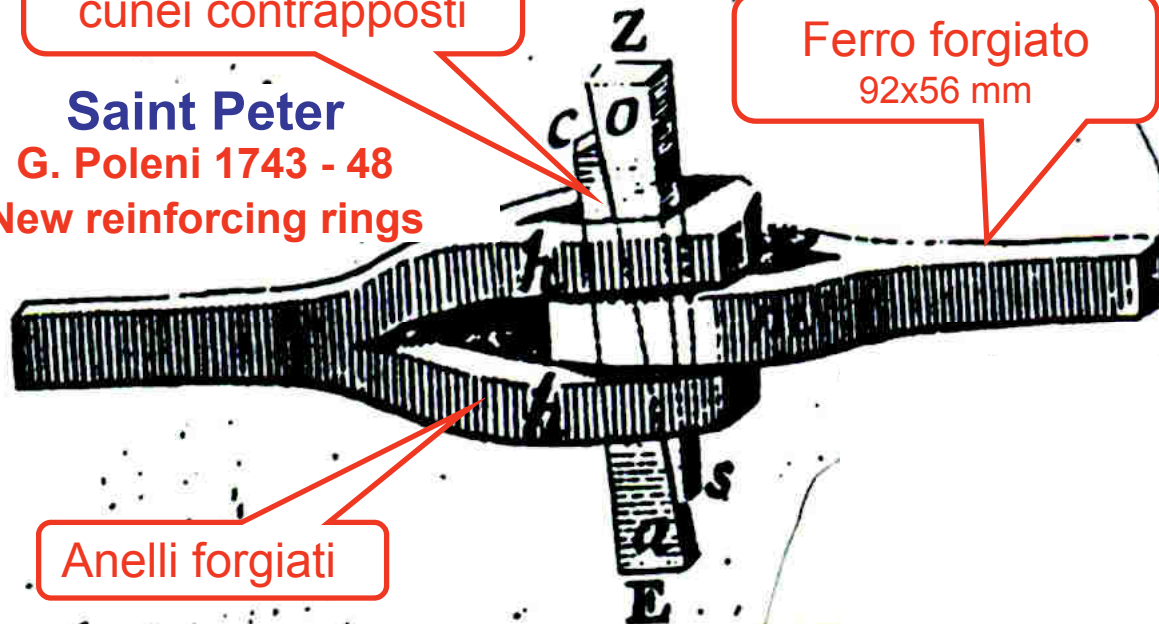


Chiavardatura a cunei contrapposti

## Saint Peter

G. Poleni 1743 - 48

New reinforcing rings



Ferro forgiato  
92x56 mm

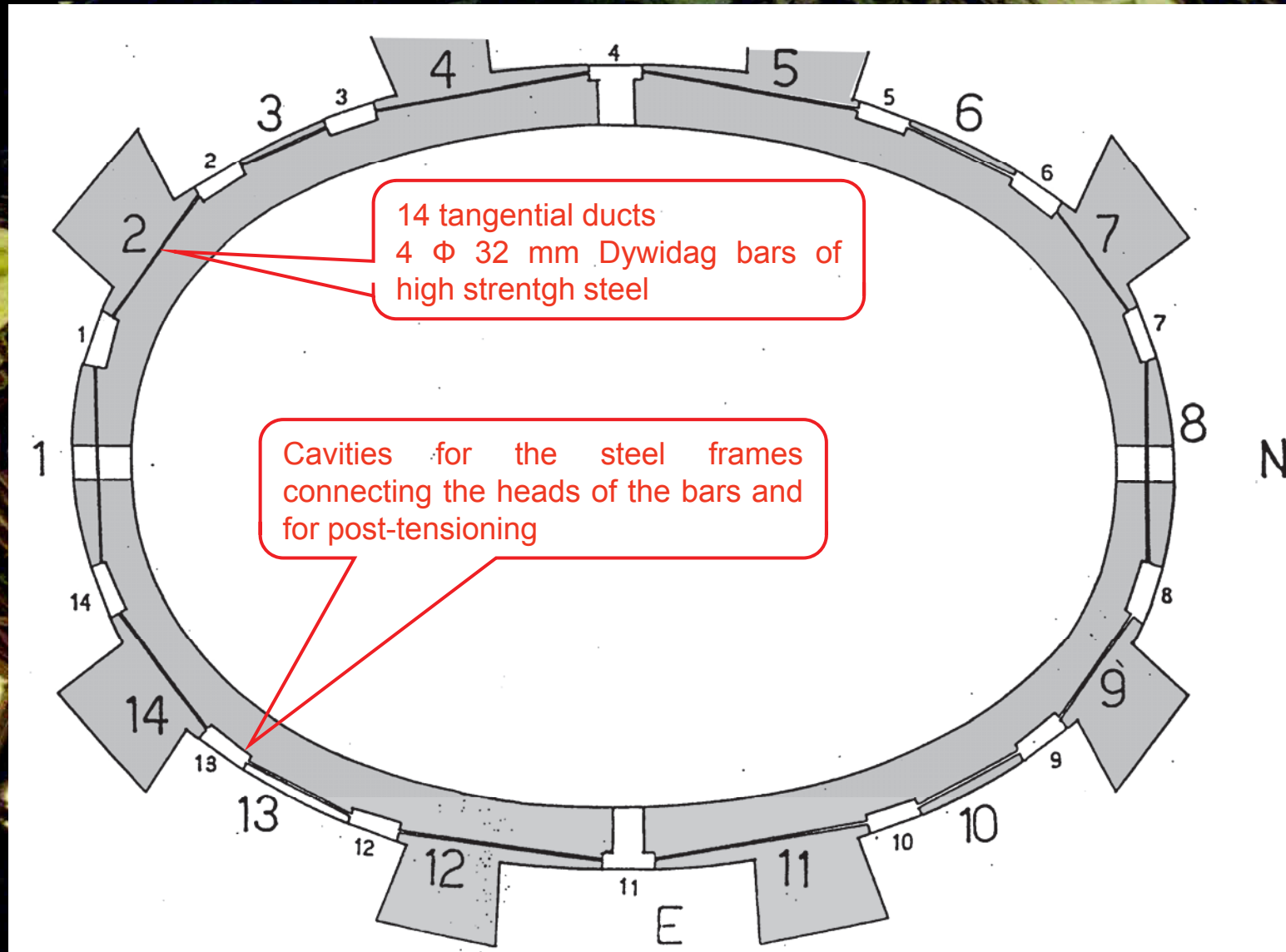
Anelli forgiati



The background of the slide is a photograph of the interior of a large, ornate dome. The dome is covered in intricate carvings and sculptures, with a central medallion and several smaller circular medallions. The lighting is dramatic, with bright spots from windows or skylights illuminating parts of the structure, while other areas are in deep shadow. The overall color palette is dark with highlights of gold and white.

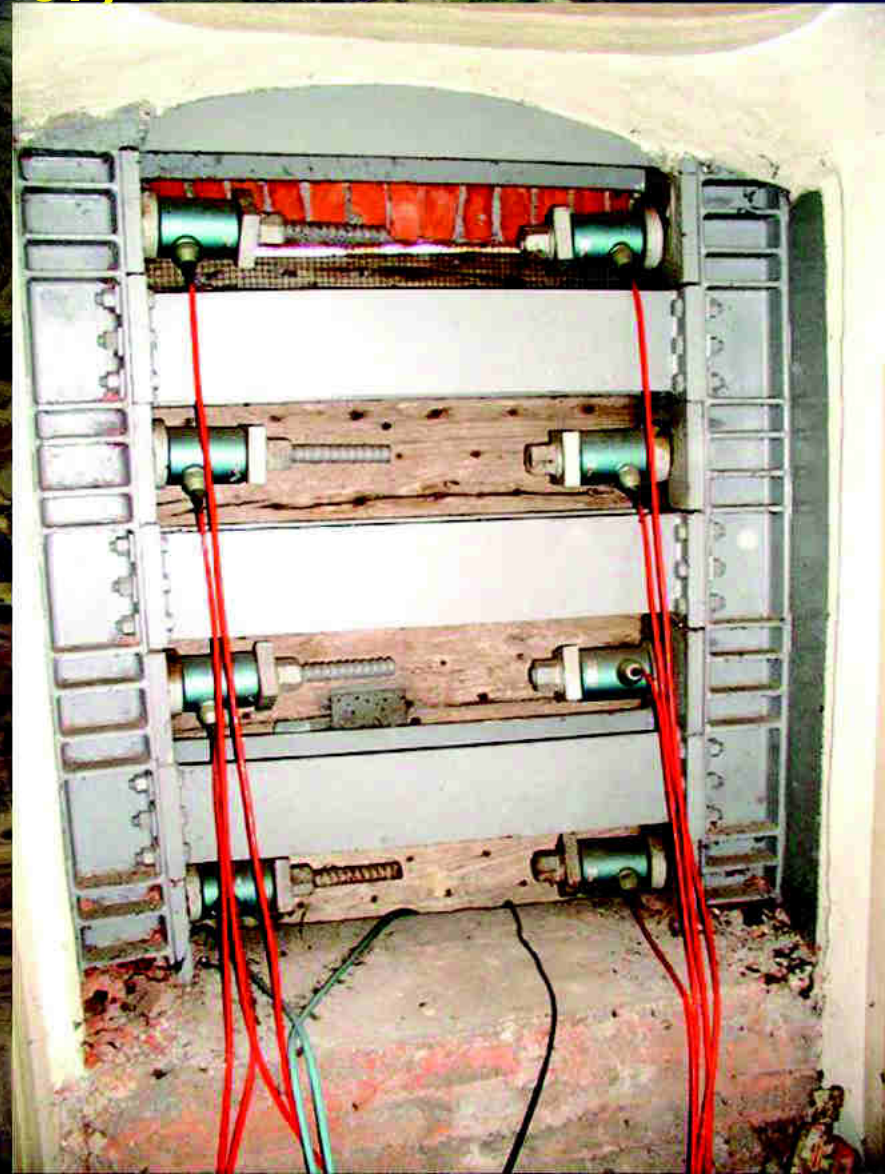
**VICOFORTE  
DESCRIPTION OF 1985  
STRENGTHENING WORKS**

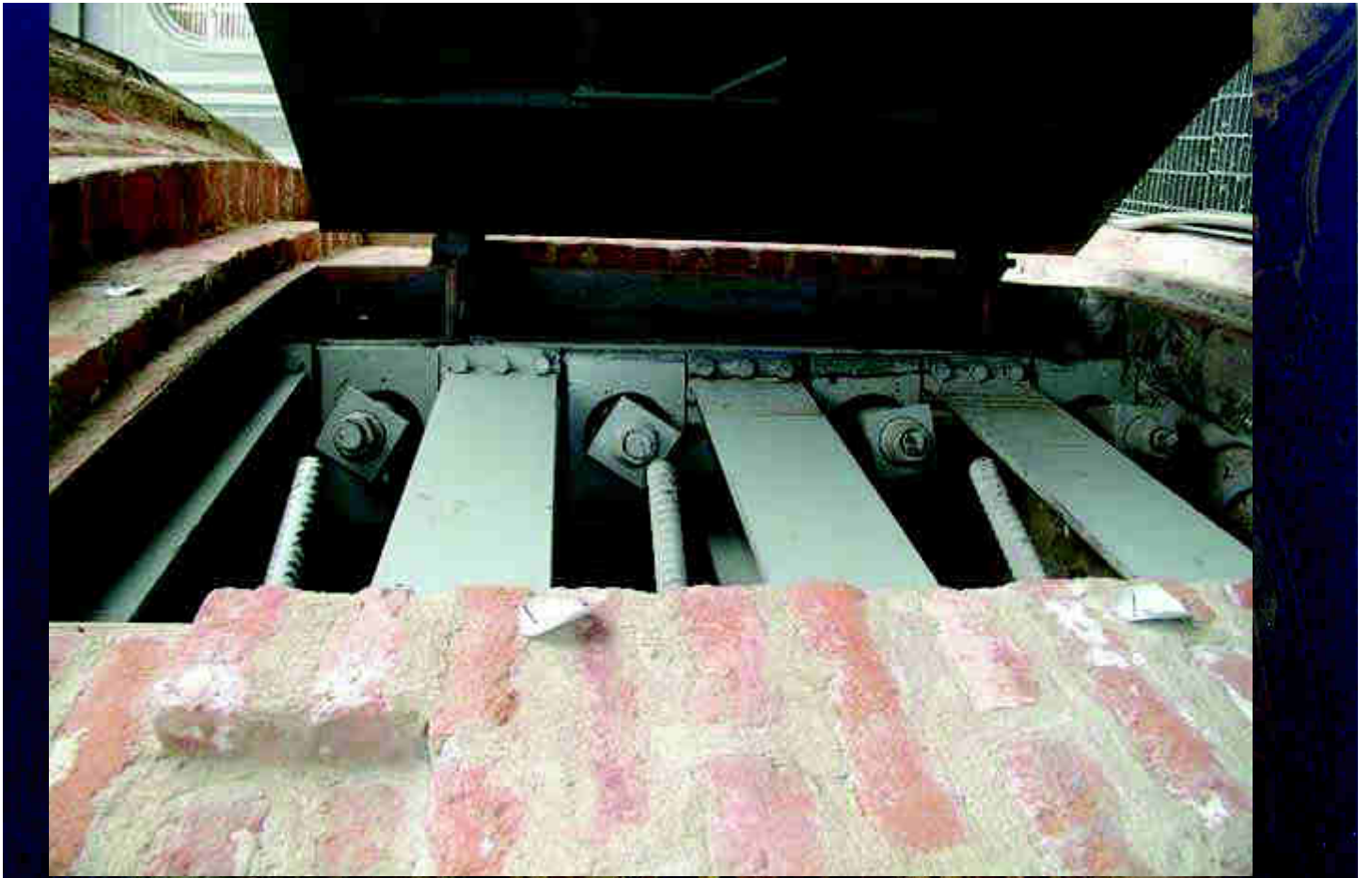
# Post-tensioning ring at the base of the dome (1985-87)



# Post-tensioning ring at the base of the dome (1985-87)


- 14 groups of tangential ties
- 4 superimposed Dywidag 32 mm bars (32 cm<sup>2</sup> in total) of high-strength steel
- each bar is located in ducts drilled in the masonry
- the 14 groups of bars are interconnected by steel trusses





The image shows the interior of a large, ornate dome, likely from a historical building. The dome is covered in intricate carvings and paintings. A ring of windows is visible near the top of the dome, and the overall lighting is warm and golden. The text "VICOFORTE RELIABILITY ASSESMENTS" is overlaid in the center in a bold, yellow, sans-serif font.

**VICOFORTE  
RELIABILITY  
ASSESMENTS**



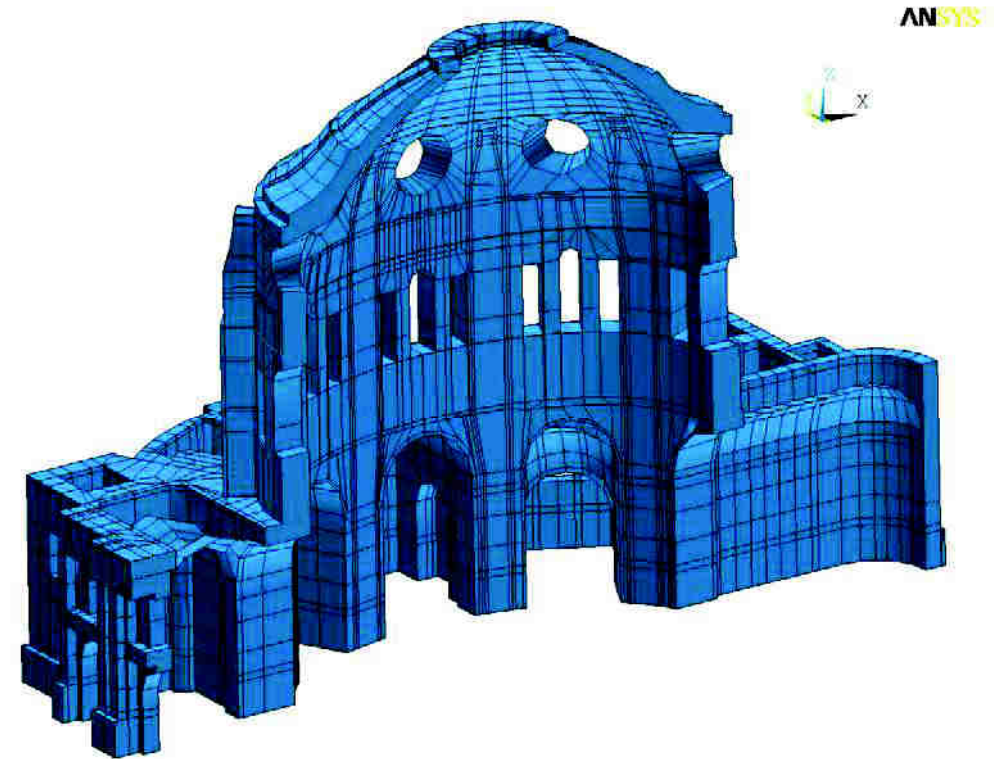
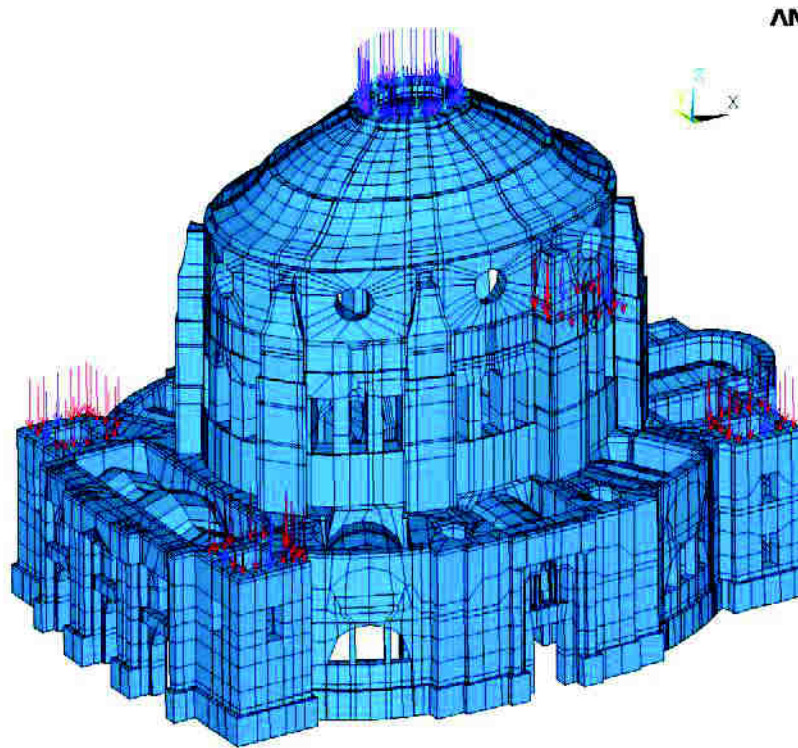
**1. Reliability assessments  
under gravity loads**



# Modeling strategies

- **Different analyses using various material and structural models, with different levels of sophistication, focusing on different aspects of the structural response:**
  - 1. Linear-elastic FEM analysis of the entire undamaged building**
  - 2. Linear-elastic FEM analysis of the damaged dome-drum system**
  - 3. Damage FEM analysis of the dome-drum system**
  - 4. Limit state analysis of the dome-drum system**

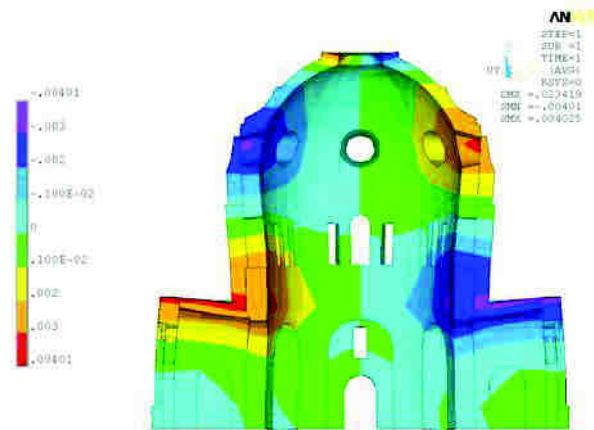
# 1. Linear-elastic FEM analysis of the entire undamaged building



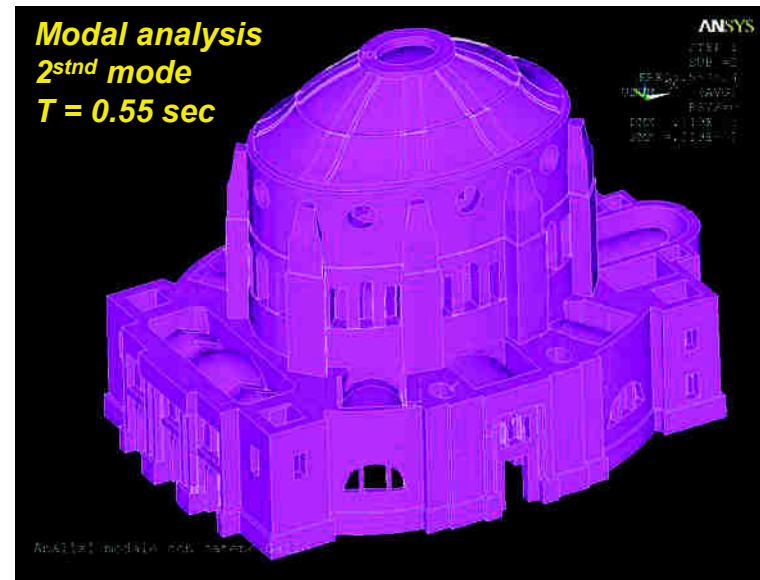
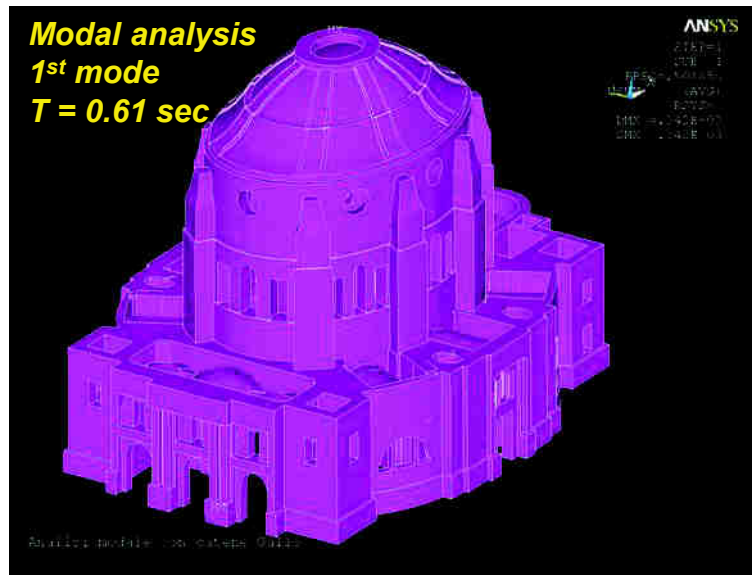
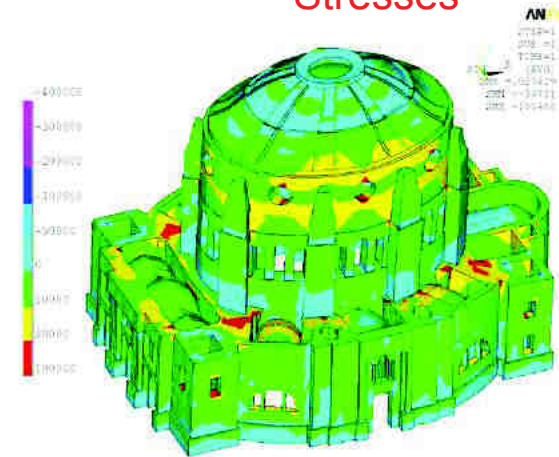
*Alberto Spadafora, Politecnico di Torino*  
Global FE linear elastic model

# 1. Linear-elastic FEM analysis of the entire undamaged building

Deformations

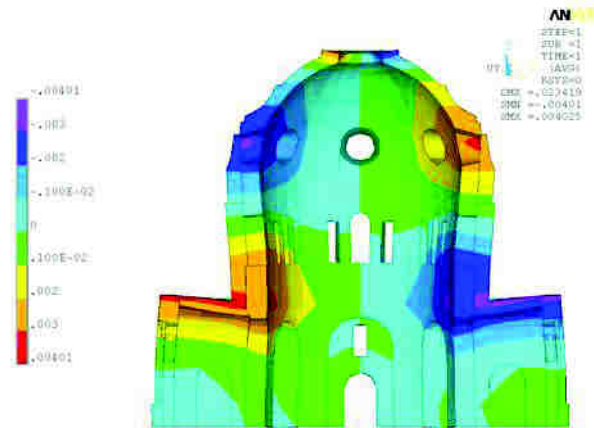


Stresses

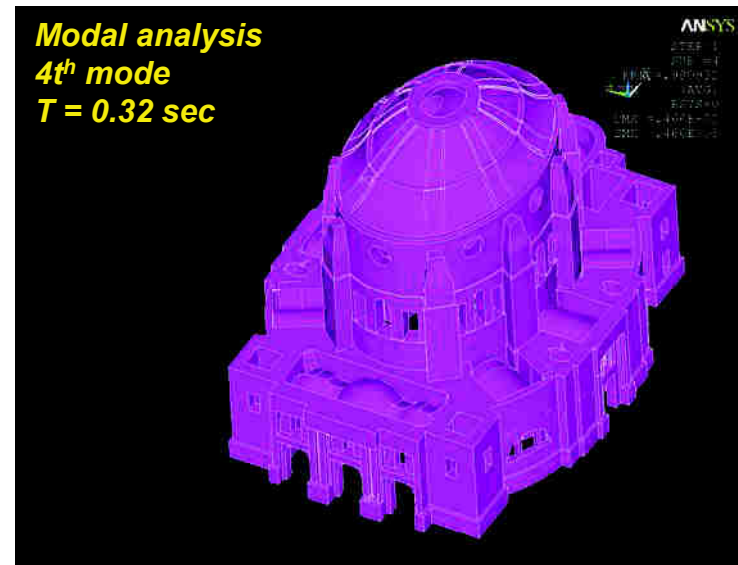
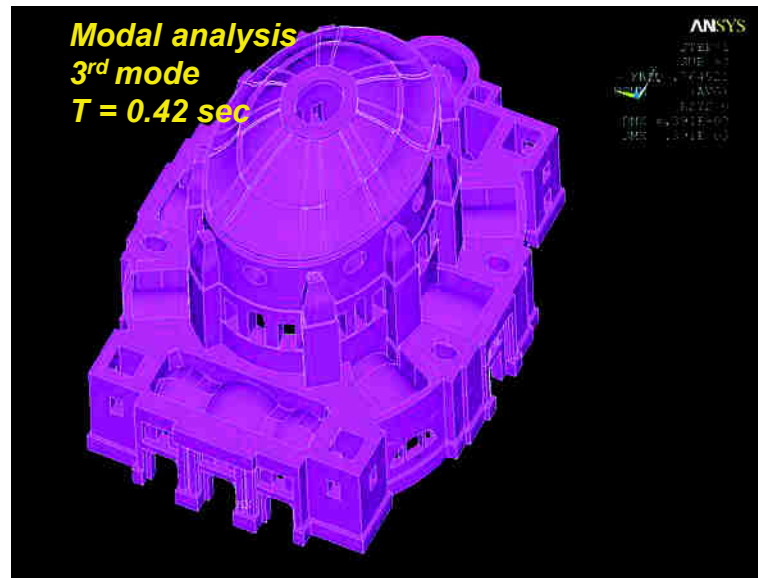
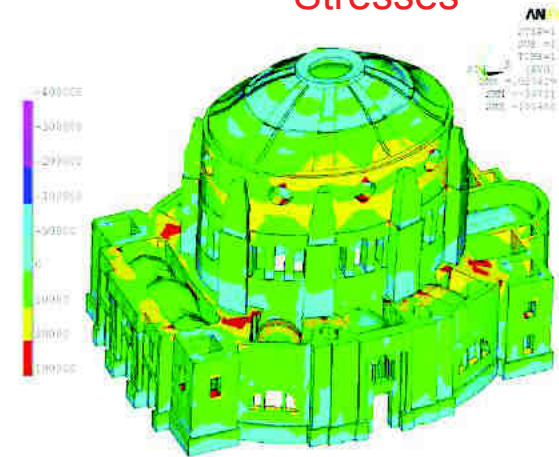


# 1. Linear-elastic FEM analysis of the entire undamaged building

Deformations



Stresses

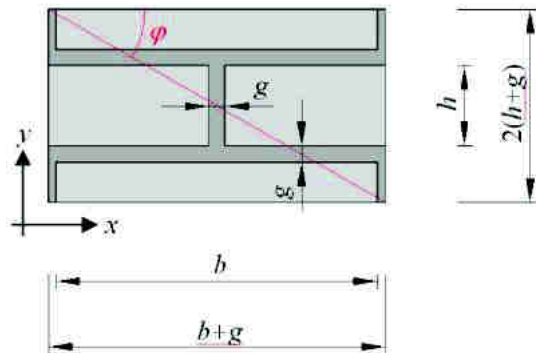


# 3. Damage FEM analysis of the dome-drum system

## THE CONSTITUTIVE MODEL

### HIPOTHESES AND GENERAL FEATURES

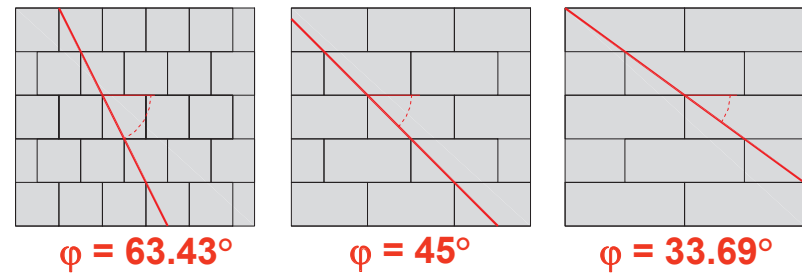
#### REFERENCE VOLUME:



#### HYPOTHESES:

- PLANE STRESS
- MORTAR JOINTS AS INTERFACES
- UNIFORM STRESSES AT INTERFACES
- MORTAR HEAD JOINTS AS GEOMETRICAL DISCONTINUITIES

#### ANGLE OF INTERLOCKING



$$\varphi = \text{tg}^{-1} \left( 2 \frac{h+g}{b+g} \right)$$

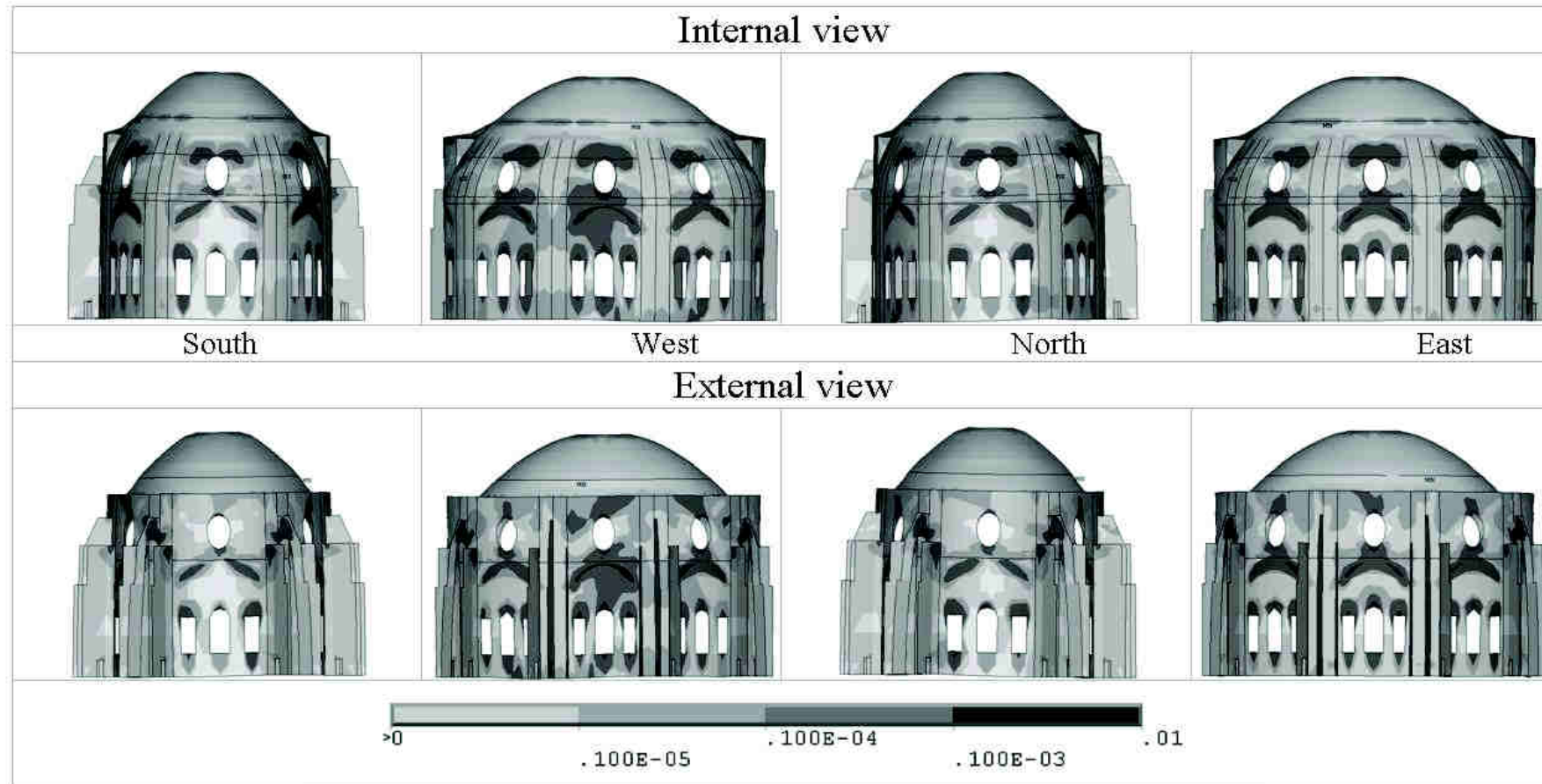
DAMAGE + FRICTION  
IN MORTAR JOINTS

DAMAGE IN BLOCKS

DAMAGE IN  
COMPRESSION

**NON LINEAR  
BEHAVIOUR**

### 3. Damage FEM analysis of the dome-drum system



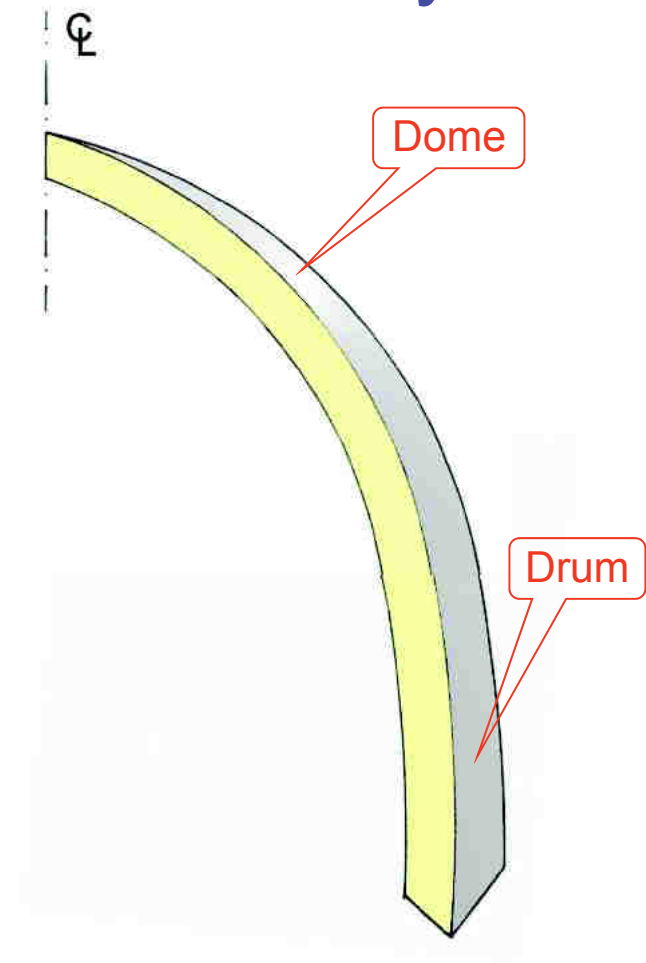
Principal inelastic strains **considering foundations settlements**



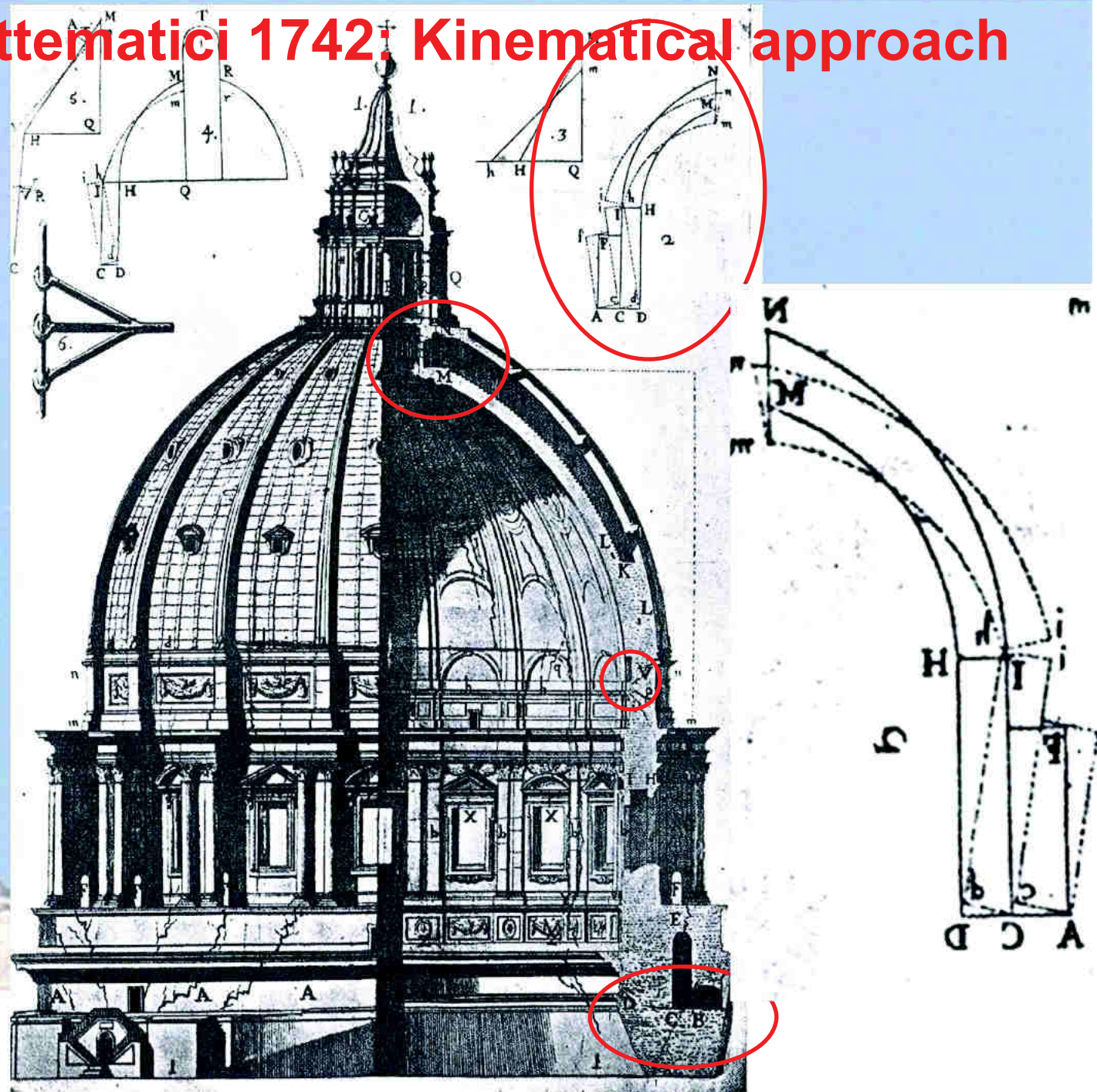
*Chiara Calderini, Università di Genova*  
Damage FEM analysis of the dome-drum system

## 4. Limit state analysis of the dome-drum system

- Assessment of the stability of a thin slice of the dome-drum system under the conservative assumption of separation by fully developed meridional cracks
- Assumptions for the masonry:
  - *No tensile strength*
  - *Unlimited compressive strength*
  - *No sliding* (Kooharian 1953, Heyman 1966)
- Application of the statical or kinematical theorem

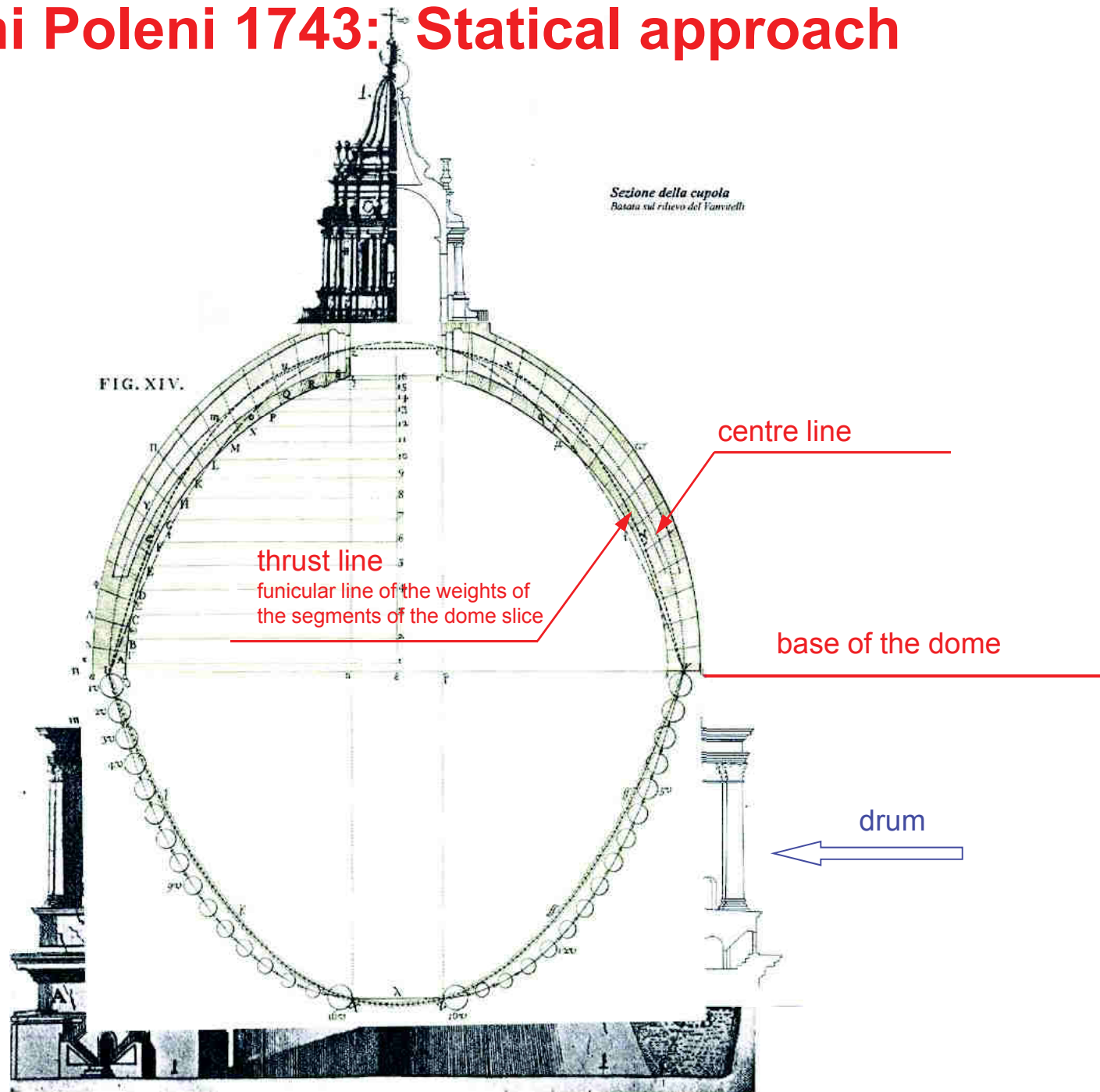


✓ I Tre Mattematici 1742: Kinematical approach



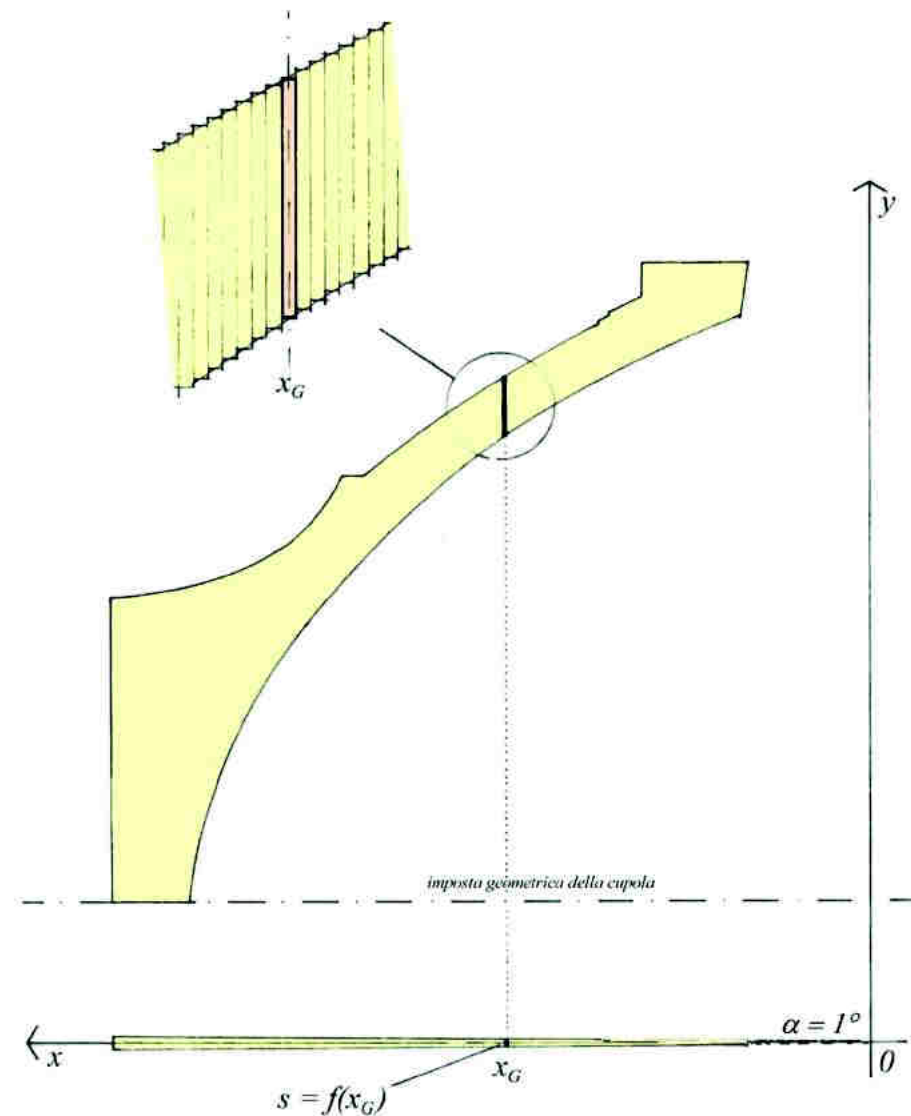


# ✓ Giovanni Poleni 1743: Statical approach



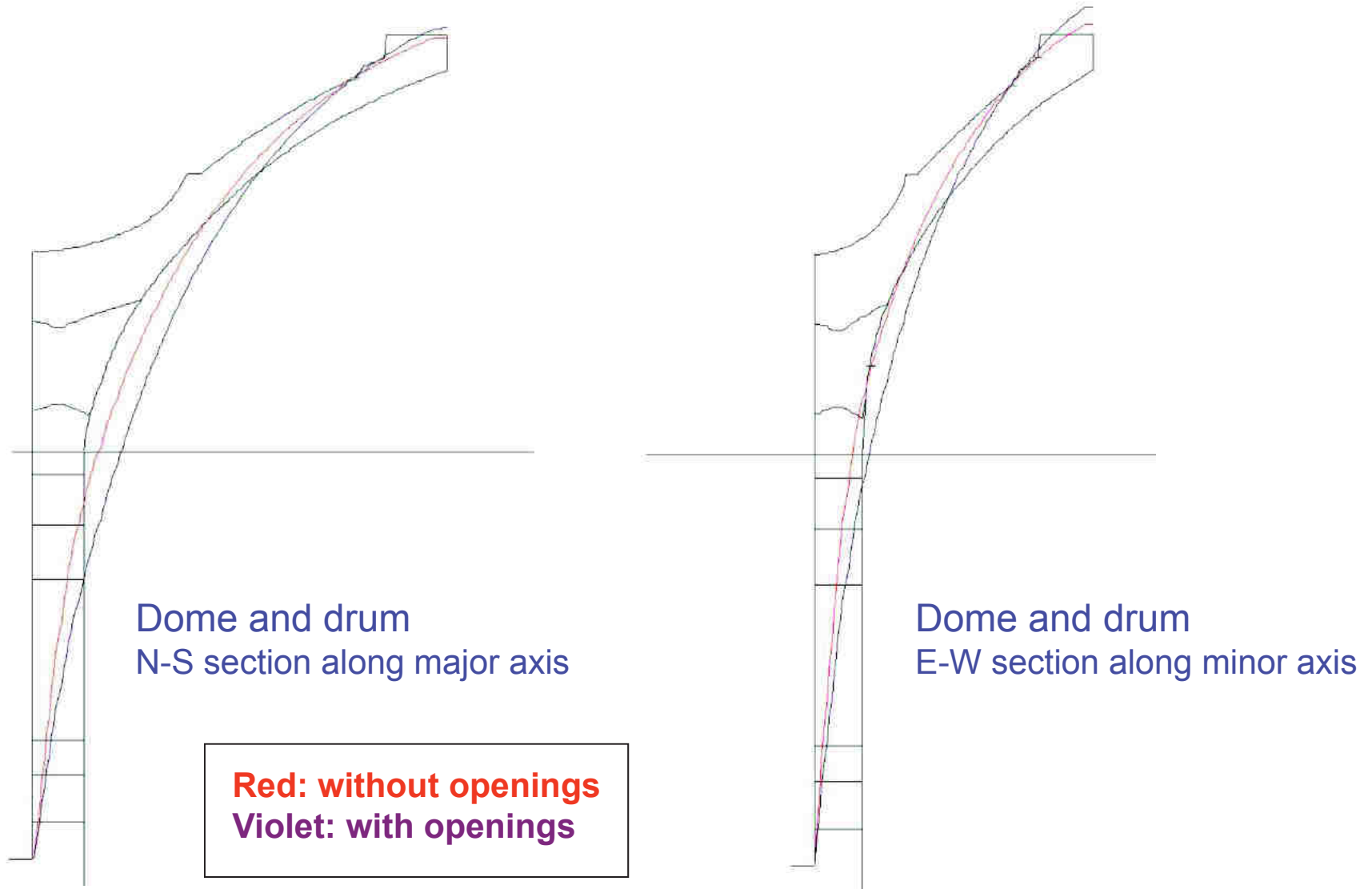
# Operational model

- Lunes of the dome and drum of  $1^\circ$  of amplitude are considered
- The structural section is divided in vertical elements of finite small dimension (0.10 m)

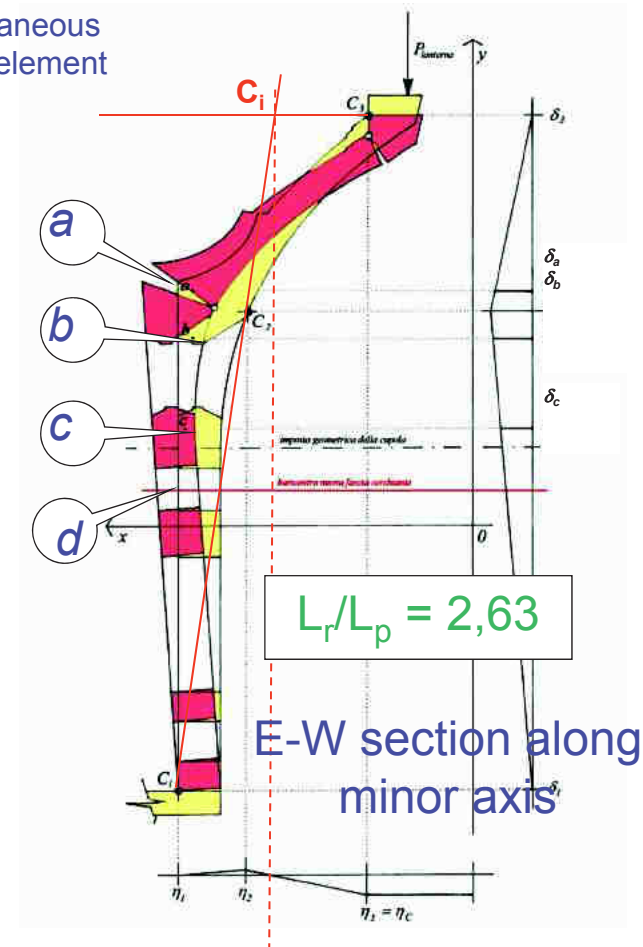
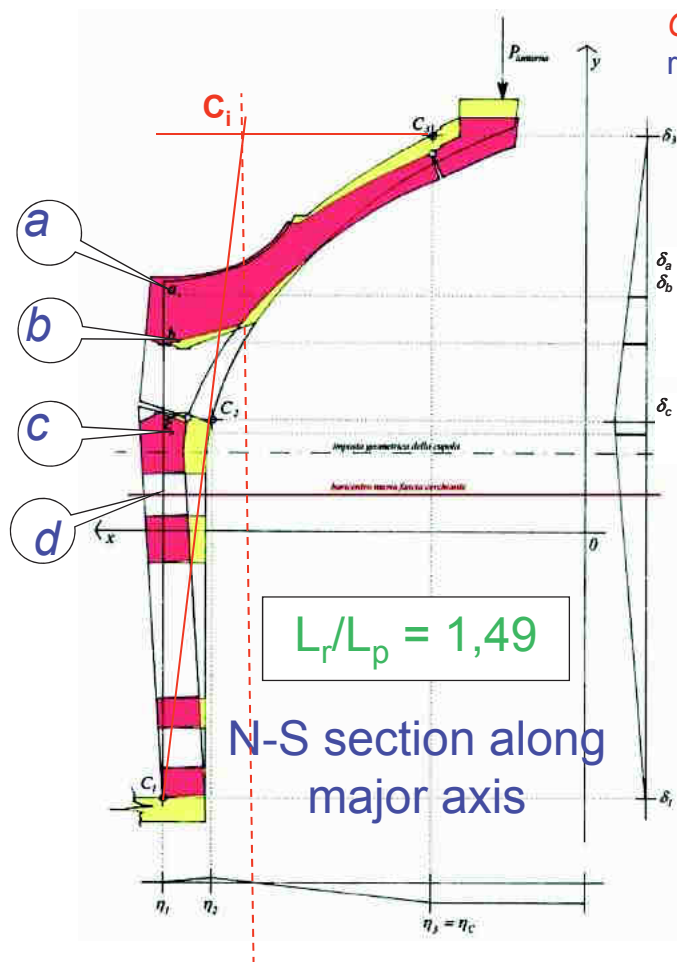


# Statical approach

The contribution of the original iron rings is ignored



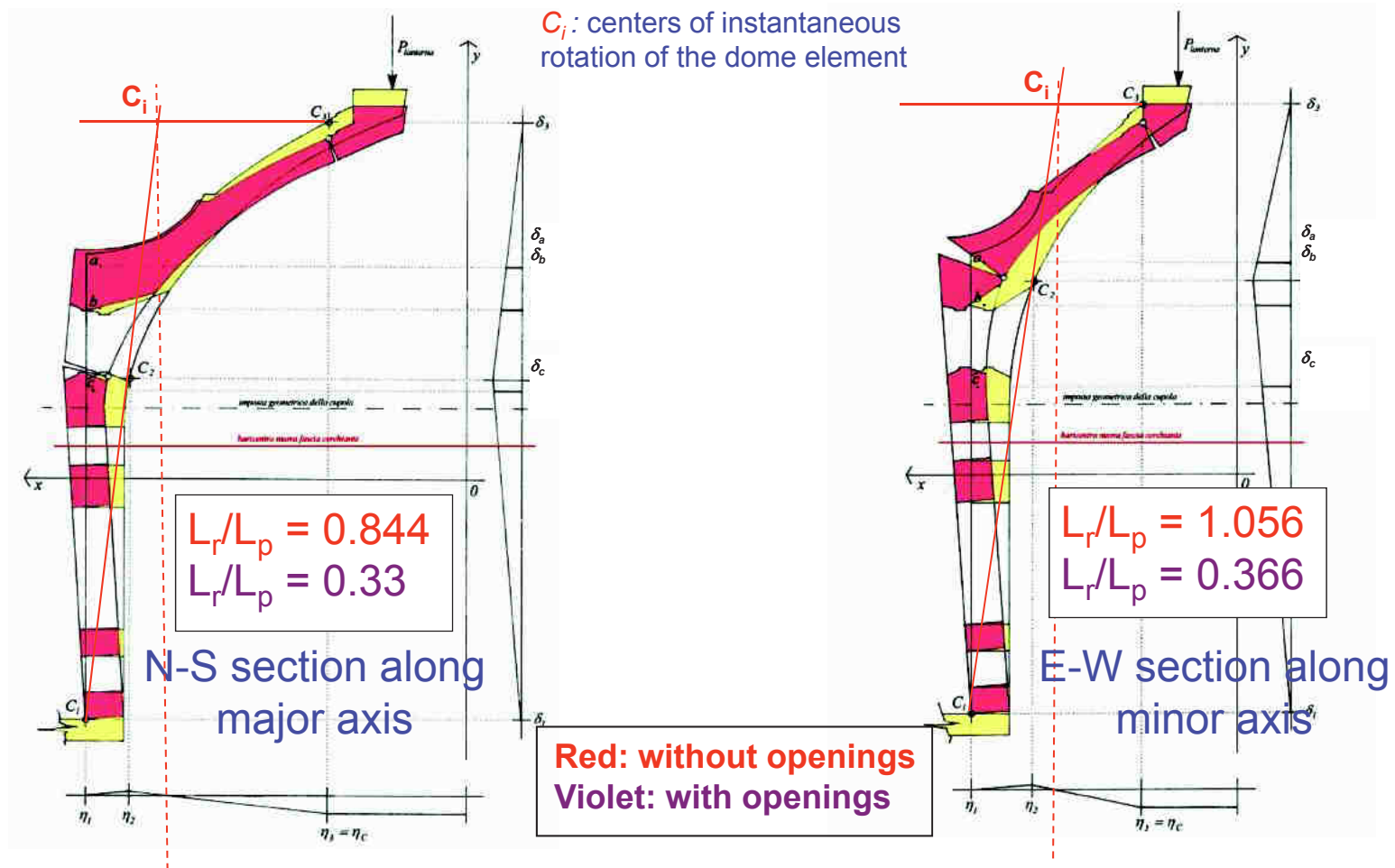
# Kinematical approach



Determination of the minimum ratio  $L_r/L_p$  between resisting and pushing virtual works taking into account the contribution of the original iron rings and the presence of window openings.

Alessandro Reffo, Politecnico di Torino

# Kinematical approach



Determination of the minimum ratio  $L_r/L_p$  between resisting and pushing virtual works ignoring the contribution of the original iron rings.

The background of the slide is a photograph of the interior of a large, ornate dome, likely St. Peter's Basilica. The dome is covered in intricate frescoes and architectural details. Light streams in from a series of windows around the base of the dome, creating a dramatic play of light and shadow. The overall color palette is dominated by warm, golden-brown and yellow tones.

## **2. Evaluation and reduction of seismic risk**

**2.1 Definition of seismic input**

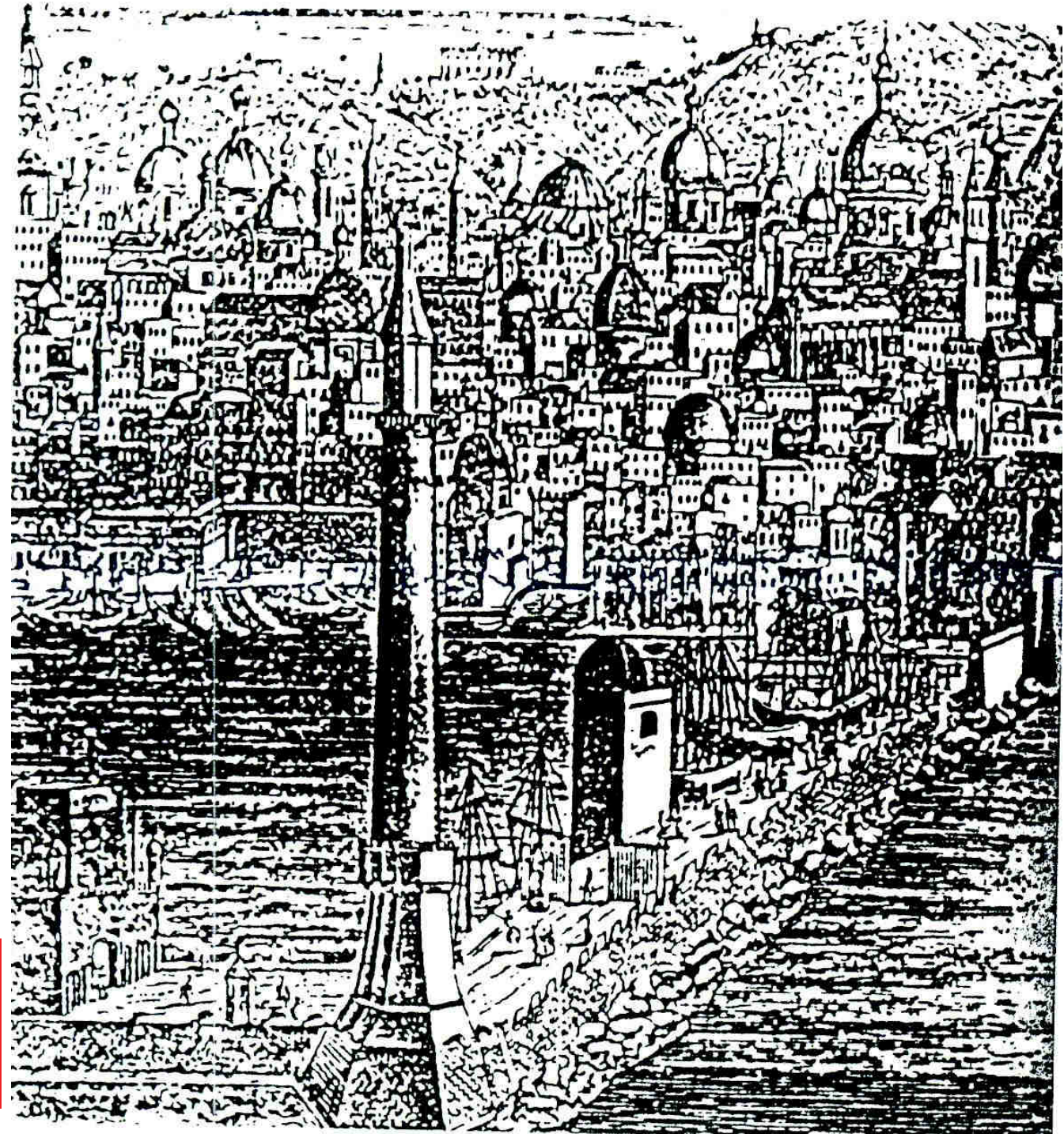
**2.2 Dynamic knowledge for the evaluation of seismic risk**

**2.3 Evaluation of seismic risk of the monument**

**Vulnerability of  
dome-drum  
systems under  
gravity and  
seismic loads**

**Just a few of these  
domes survive today**

**Wernot  
View of Naples  
around 1700**



An aerial photograph of a densely packed town with terracotta roofs. In the center, a large, light-colored dome-drum structure is visible, showing significant damage and structural failure. The dome is partially collapsed, and the drum is exposed. The surrounding buildings are mostly multi-story structures with tiled roofs. A large green tree is visible on the left side of the dome structure.

**Seismic vulnerability of  
dome-drum systems in the  
recent l'Aquila-Abuzzi  
earthquake  
(april 2009)**



# S. Maria Paganica





*Santa Maria del Suffragio*



S. Agostino

S. Agostino



## 2. Evaluation and reduction of seismic risk

### *Introductory comment*

- In Italy **seismic classification** has progressively been extended from about **15-20%** of the country after the big earthquakes at the beginning of past century (Messina 1908, southern Italy 1915) to about **60-70 %** of the nation in the '80s, and to the **whole geographical area since 2003** (after the 2002 Puglie earthquake).
- Italy, like India, is recognized as one the most important “container” of cultural and architectural heritage the world over
- Consequently, the problem of safeguarding for future generations this heritage in a seismic active zone arises
- In 2006, as a result of joint work between the Ministry of Cultural Heritage, the Seismic Protection Department of the central government and the Universities, ***Italian Guidelines for the evaluation and reduction of seismic risk of cultural heritage*** have been edited (revised 2008, 2011, see Part 1) .
- The joint project of **Evaluation and reduction of seismic risk for Vicoforte**, coordinated by the Politecnico di Torino, in cooperation with the Universities of Pavia (IUSS Eucentre and ROSE School) and of Genoa, intends to be an advanced model project, to be proposed as a **model format for other important monuments**

## 2. Evaluation and reduction of seismic risk

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- This need was well evidenced by the severe losses of architectural masterpieces in earthquakes that in recent years hit Assisi (1997) and Abruzzo region (2009). In the second event, the **high vulnerability of dome-drum systems** was demonstrated by the collapse or great damage of quite a few of them.
- The joint project of **Evaluation and reduction of seismic risk for Vicoforte**, coordinated by the Politecnico di Torino, in cooperation with the Universities of

## Evaluation of seismic risk

A wider attention has been given in recent years to the **conservation of cultural heritage in seismic areas**. **Guidance documents** have been developed for countries characterized by an exceptional cultural heritage and by significant seismicity, like Italy (Directive PCM).

**Directive PCM** underscores the importance of an **assessment and mitigation of seismic risk based on good structural knowledge of cultural heritage**. This need was well evidenced by the severe losses of architectural masterpieces in earthquakes that in recent years hit Assisi (1997) and Abruzzo region (2009). In the second event, the **high vulnerability of dome-drum systems** was demonstrated by the collapse or great damage of quite a few of them.

The Basilica at Vicoforte has been chosen as a **case study for the evaluation of its seismic risk with reference to the guidance criteria of the Directive**, in the frame of an agreement with Italian Ministry for Cultural Heritage.



Earthquake in Abruzzo region

## 2.1 Definition of seismic input





## Definition of the seismic input

The research was articulated in two phases:

### 1) Site-specific Probabilistic Seismic Hazard Analysis (PSHA) and Deterministic Seismic Hazard Analysis (DSHA)

The output of the PSHA consists of probabilistic uniform hazard acceleration spectra at the site, for different reference return periods.

A number of recorded spectrum-compatible accelerograms were selected as inputs for ground response analysis.

Horizontal PGA, for a return period of 475 years = 0.096 g

Horizontal PGA, for a return period of 2475 years = 0.160 g

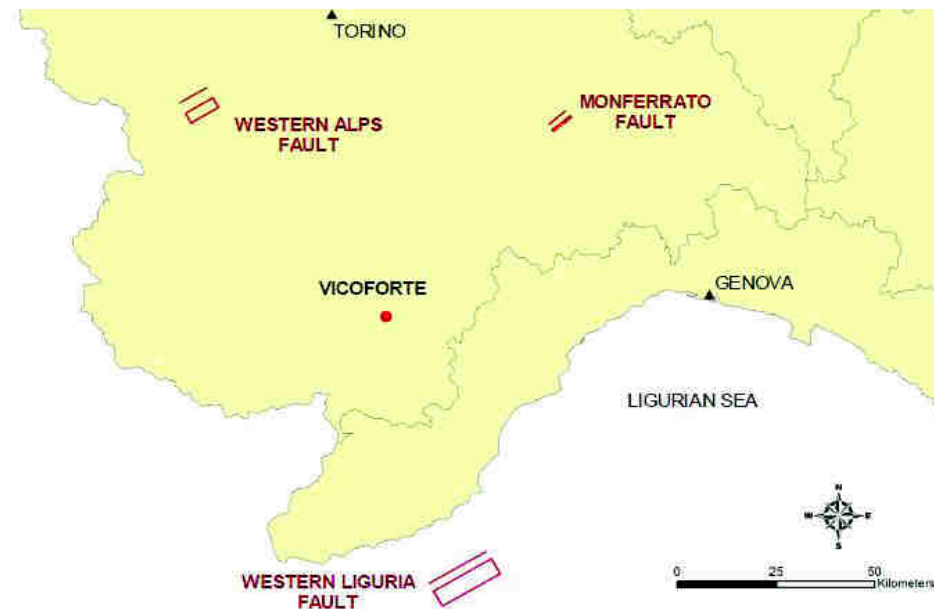


Site of low seismicity with sources located distant from the site

The DSHA was adopted to define **the worst shaking** scenario which would occur in the future, compatibly with the **tectonic and seismic setting of the region**.

To this aim, the main seismic sources in the area of interest were identified on the bases of past earthquakes and a tectonic setting and finite faults numerical analyses were performed .

**The probabilistic approach provides more severe ground shaking scenarios with respect to deterministic methods.**



Map of the area of interest with the surface projections of fault planes considered for computation of ground shaking scenarios

## 2) Investigation of the seismic site response through 1D stochastic and 2D deterministic approaches, in order to evaluate possible amplification effects due to localized lithostratigraphic characteristics at the site

To this aim, a **3D subsoil model** was constructed, integrating the results of the different geotechnical investigation campaigns.

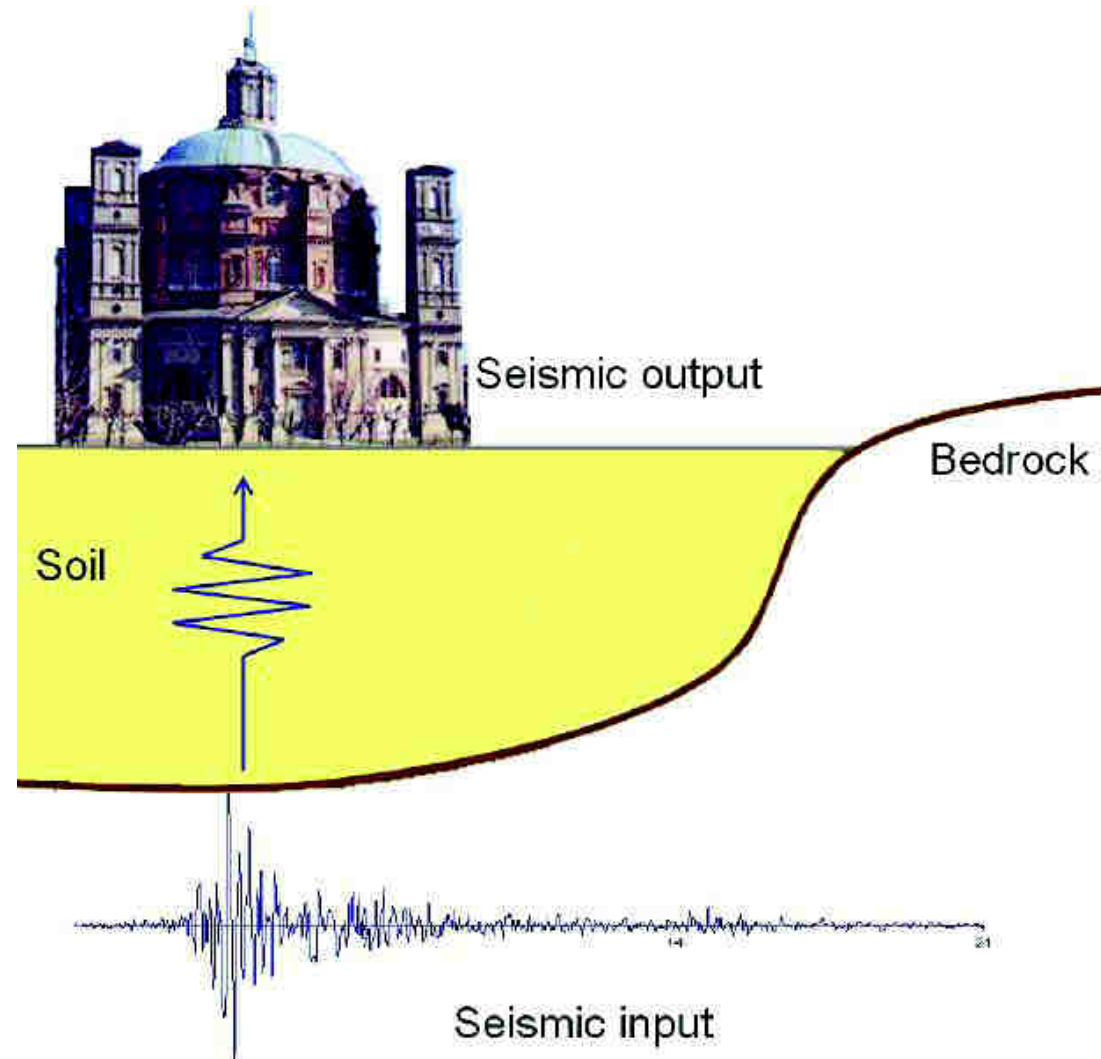
From the **1D stochastic approach**, the mean PGA at the free surface for the 475 years return period results equal to 0.2 g.



**Amplification of about 2 with respect to the PGA at the outcropping bedrock.**

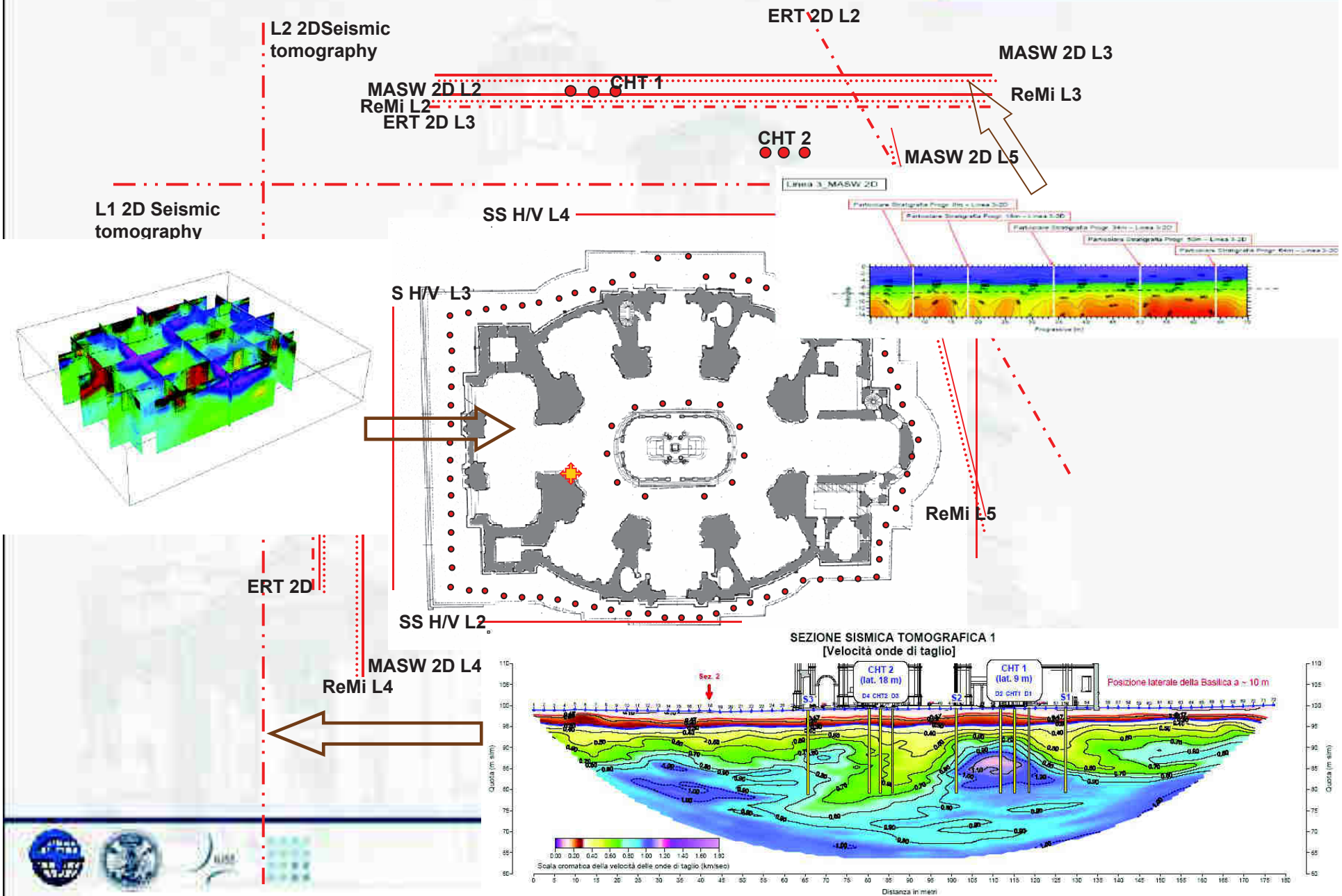
Some **amplification phenomena** are observed from the results of the **2D deterministic** ground response analysis also.

Finally, as an output of the study, **dynamic impedances** at the foundation of the Basilica were computed to be used in **soil structure interaction analysis**.



Influence of site conditions on the seismic response

# GEOTECHNICAL SITE CHARACTERIZATION



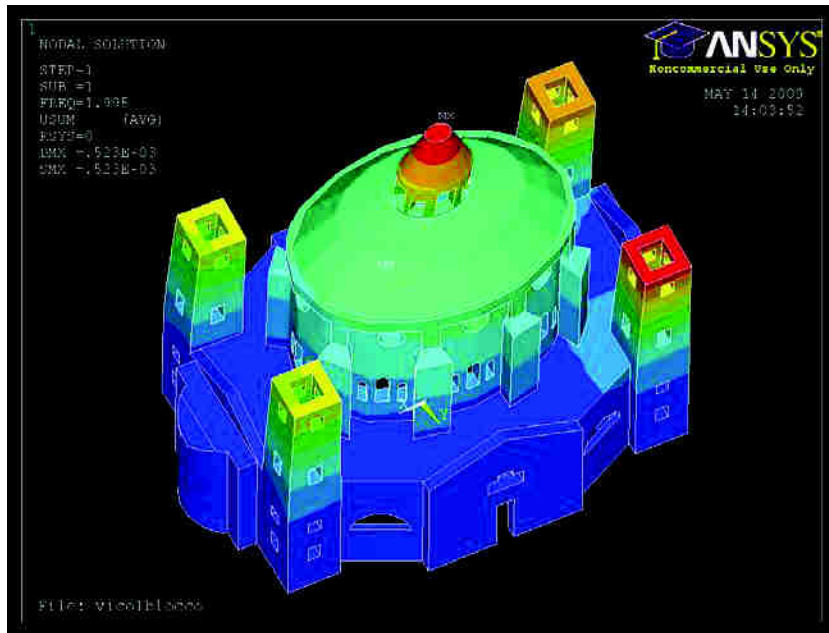


## 2.2 Dynamic knowledge for the evaluation of seismic risk

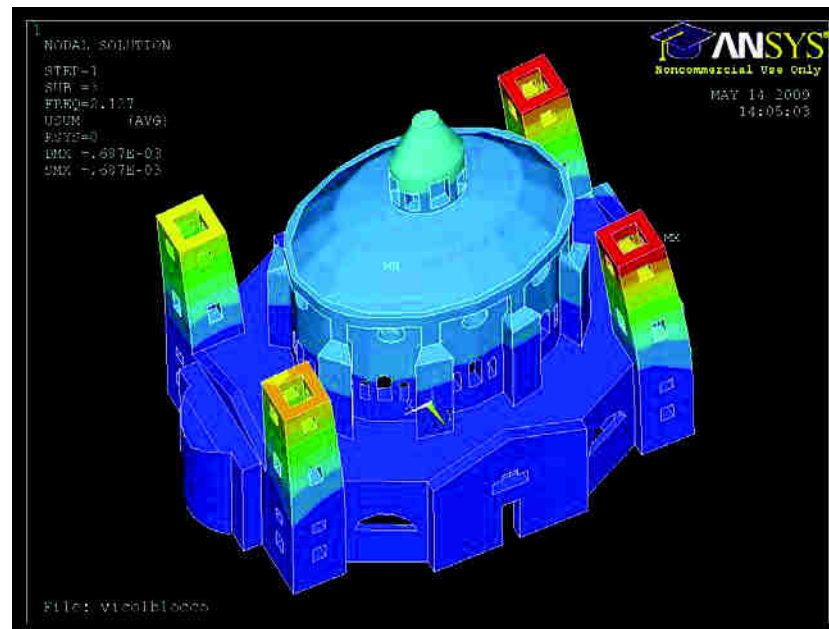
## SAFELY ATTRIBUTED SHAPES: CALIBRATED MODEL

Legend: **contour plot ANSYS :**

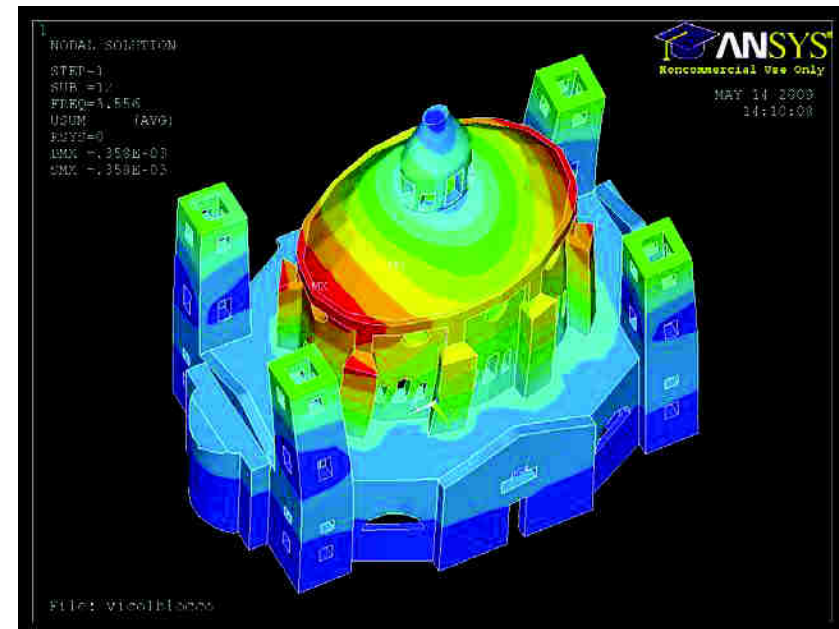
- Mode 1 = Y displacement
- Mode 3 = X displacement
- Mode 12 = Total displacement



*1° Bending along Y (MODE 1)*



*1° Bending along X (MODE 3)*



*1° Torsion of the dome (MODE 12)*

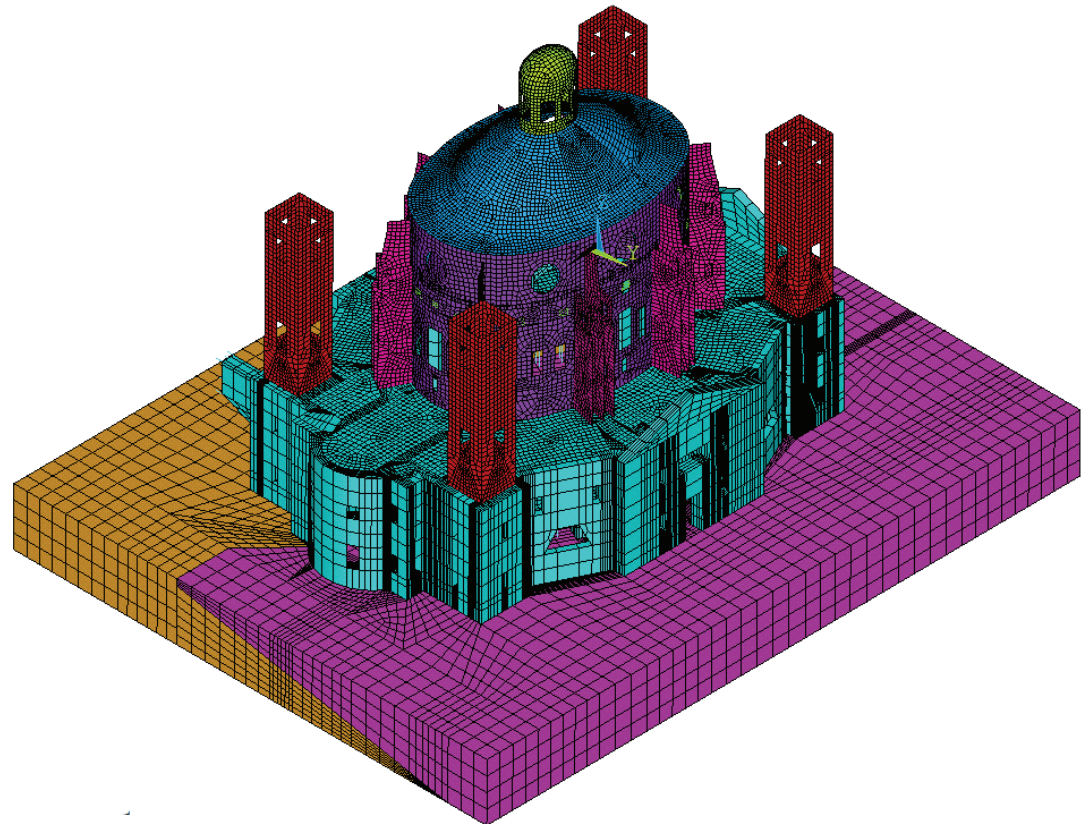
## *The Soil Structure Interaction SSI FE model*



A total of 9 different materials

- Dome
- Drum
- Bell-towers
- Buttresses
- Lantern
- Basement
- Iron-ties
- Marlstone
- Clay

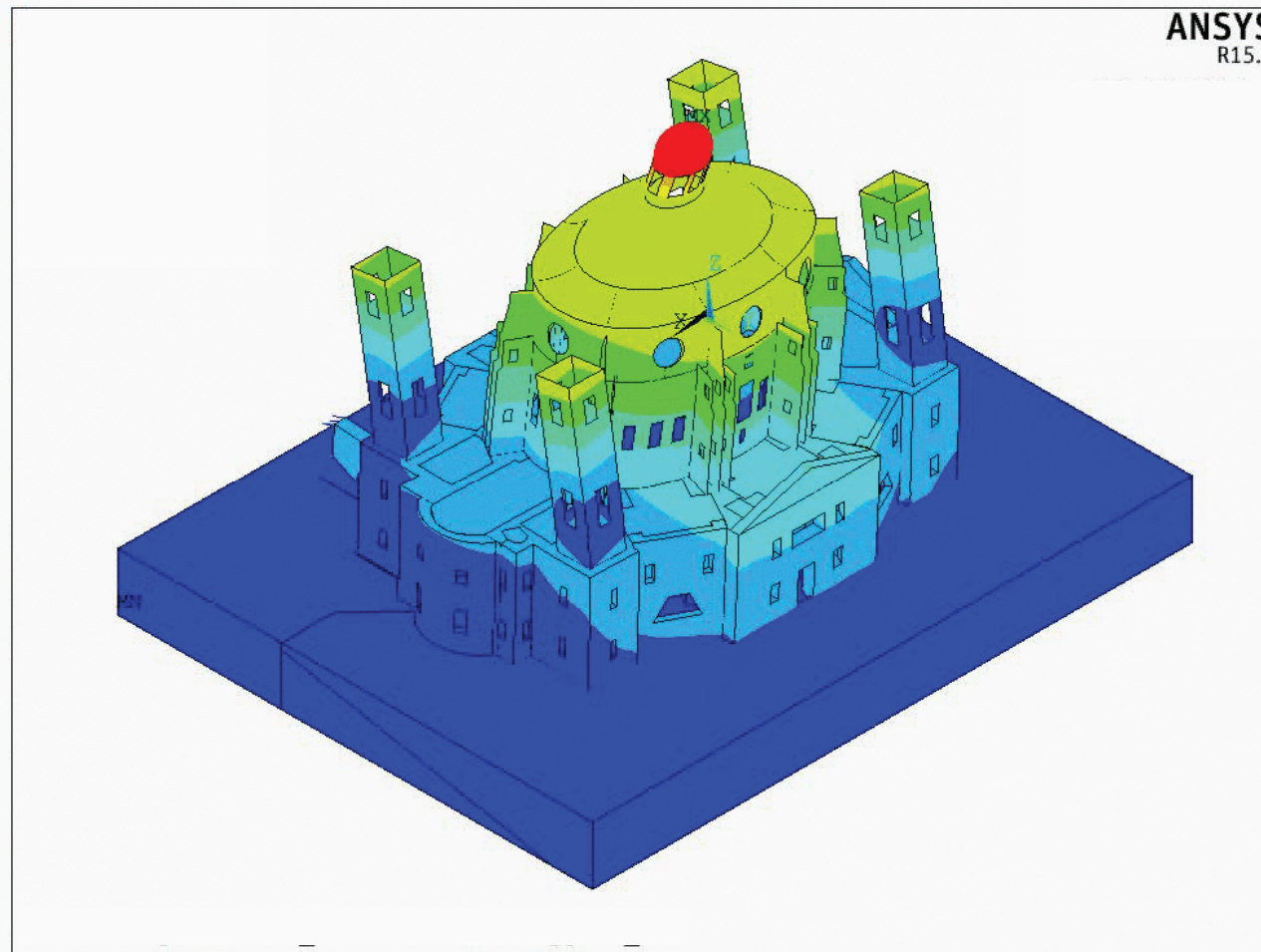
Elastic linear isotropic model:

- Solid elements for the soil and the basement
- Shell elements for the rest of the structure
- Link for the strengthening system



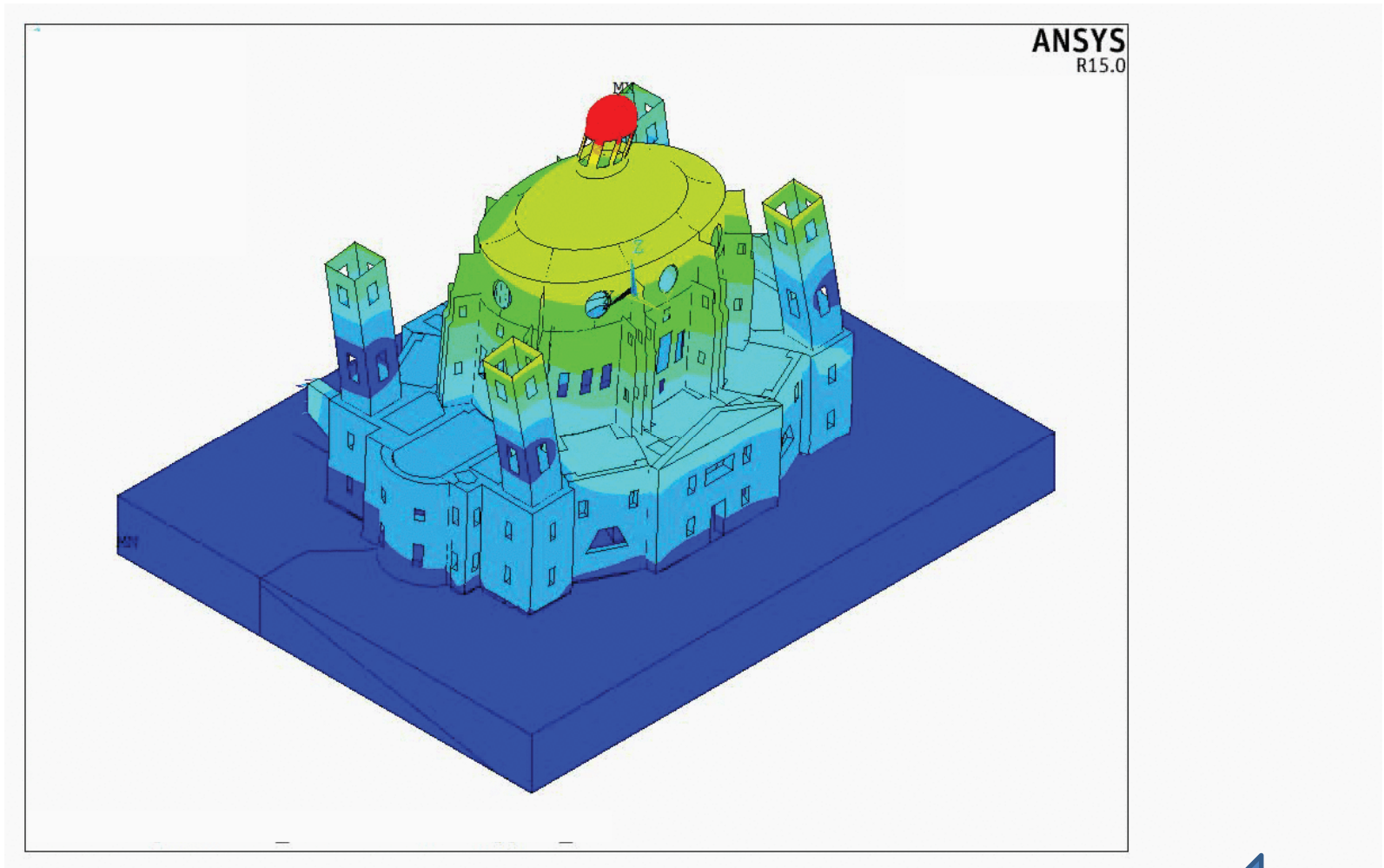
- 
- The introduction of the soil in the model (*Soil Structure Interaction SSI FE model*) allowed for a better calibration of the dynamic model.
  - The new SSI dynamic model has been used for sensor placement of a *Structural Health Monitoring (SHM)* system and will be used to study the effect of the bar strengthening system in the hypothesis of a semi-active control technology system.
- 

*1<sup>st</sup> flexural mode (1.99 Hz)*

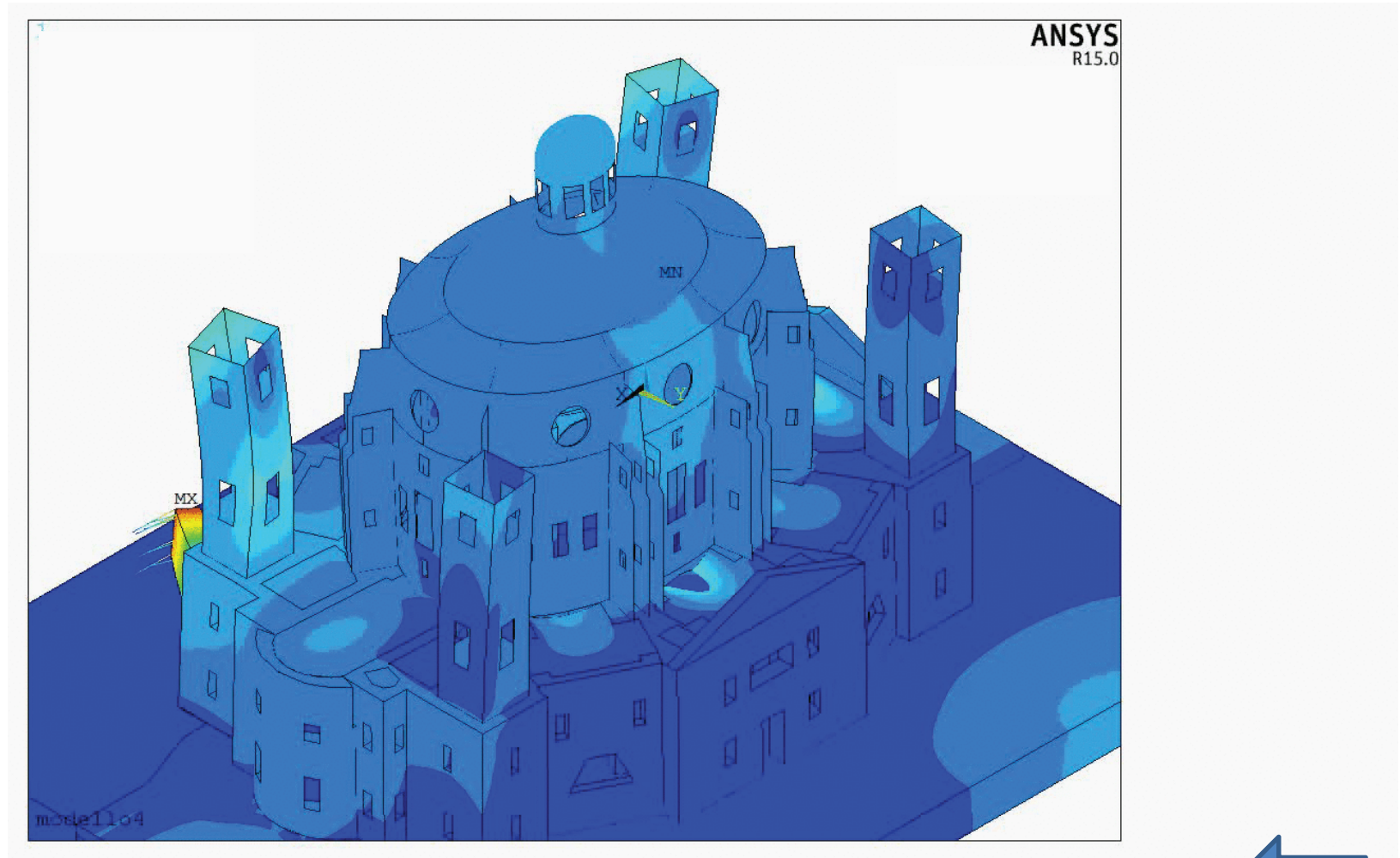




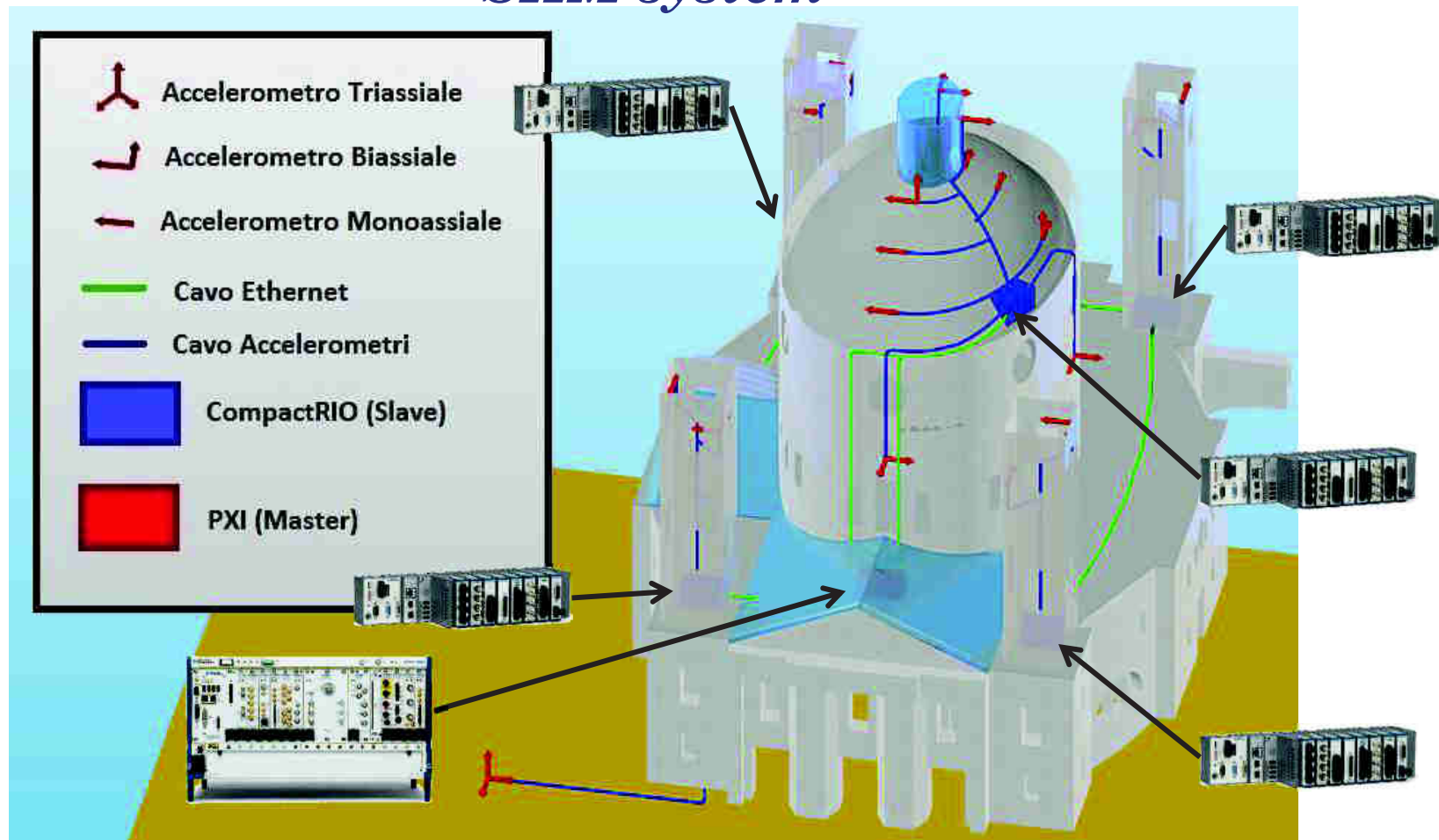
*2<sup>nd</sup> flexural mode (2.08 Hz)*



# *1<sup>st</sup> Vertical mode (6.02 Hz)*




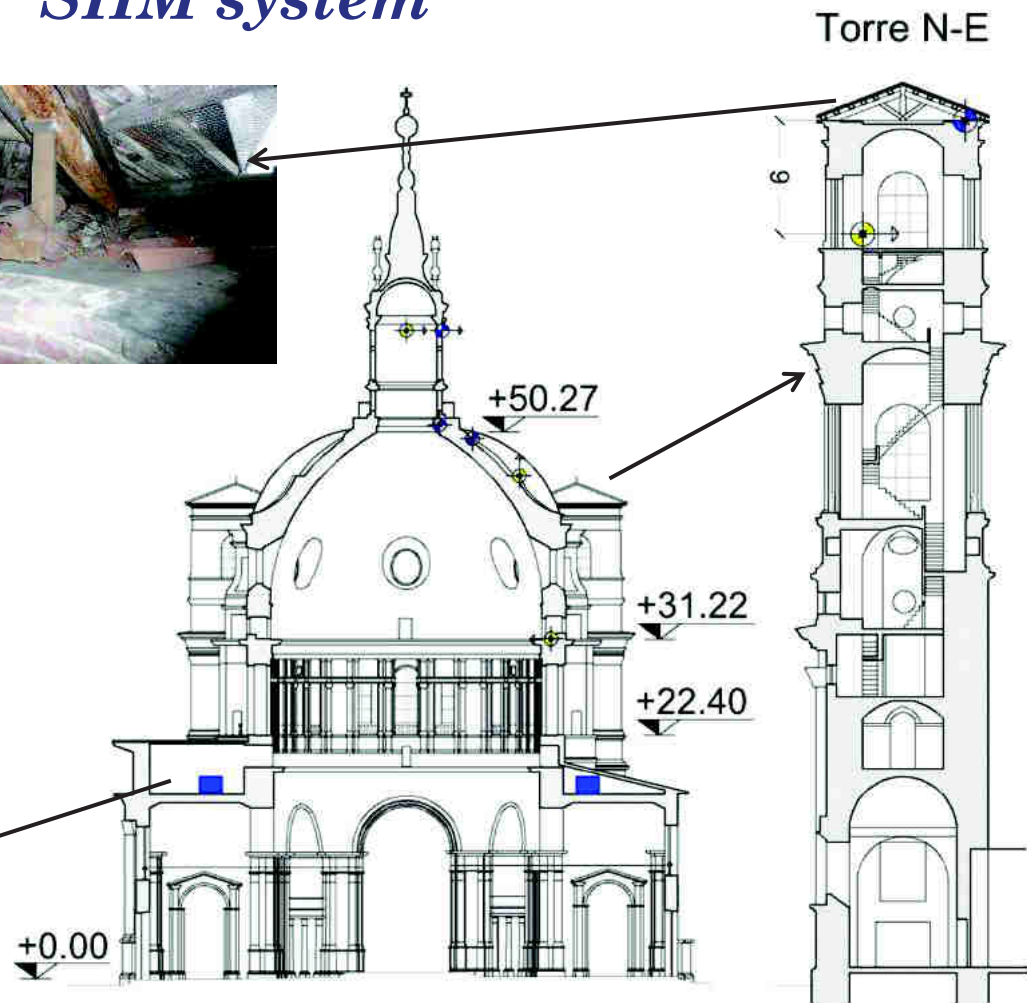
# *A new dynamic Structural Health Monitoring SHM system*



# *A new dynamic Structural Health Monitoring SHM system*

## LEGENDA:

-  Accelerometro Triassiale
-  Accelerometro Biassiale
-  Accelerometro Monoassiale
-  CompactRIO
-  PXI



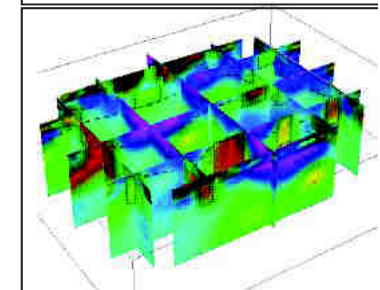
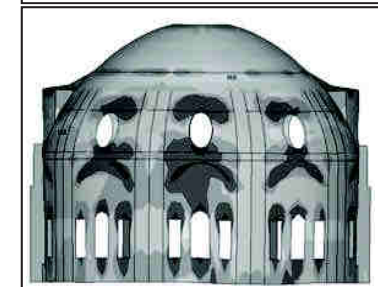
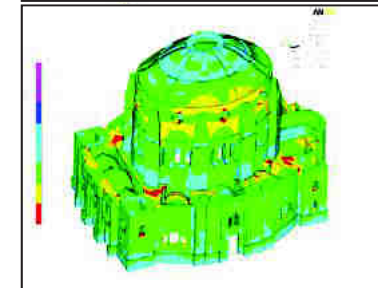
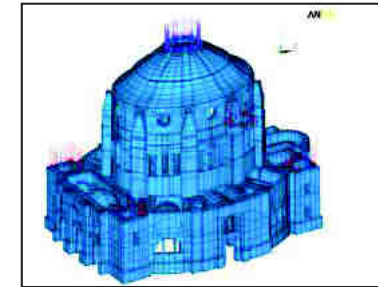
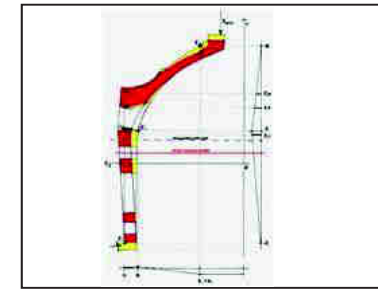
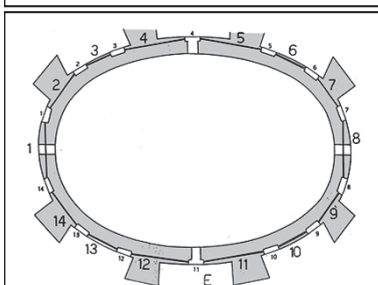
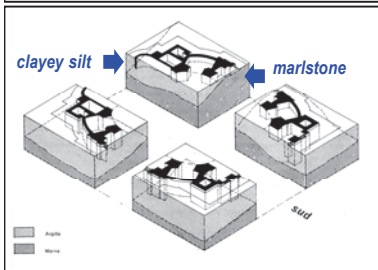


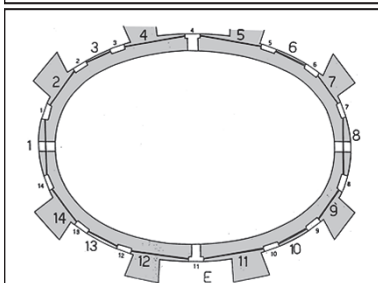
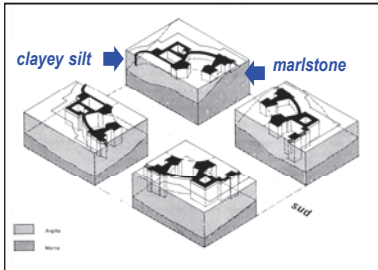
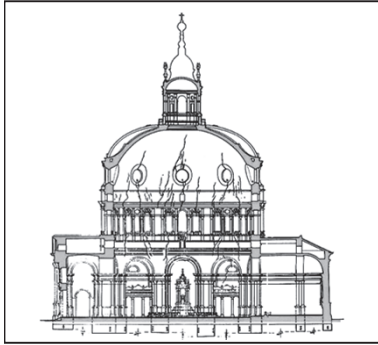
## **2.3 Evaluation of seismic risk of the monument**

**Work in progress....**

# CONCLUSIONS

- The contribution of structural engineering and geotechnics to the conservation of historical monuments is significant
- In particular in ambients like the Italian ambient containing one of the most important cultural/architectural heritage, in the world in a region which is seismically active
- The case case study of the survey and structural modeling for the reliability assessment of the world's largest elliptical masonry dome at Vicoforte, Italy, fits in this perspective, and is intended to be proposed as a scholastic case study of advanced approaches within international debate





Scuola di Dottorato del  
Politecnico di Torino  
Dottorato in Beni Culturali



# THANK YOU